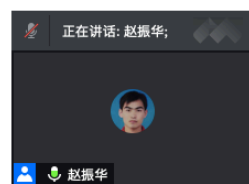


Charm Physics at BESIII

Bai-Cian Ke
Shanxi Normal University



@ 04/27/2021

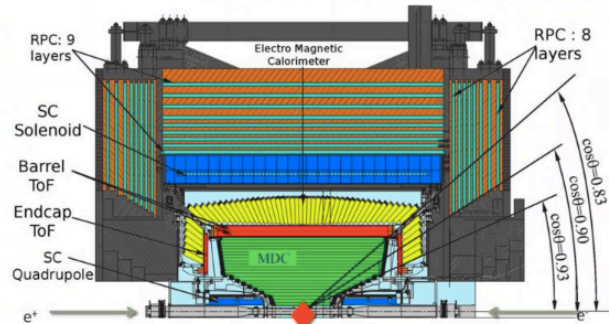


Outline

- Introduction
 - D^0 , D^+ , and D_s Dataset
 - DTag
- (Semi-) leptonic decays of $D^{0(+)}$ (by Ke Liu)
- (Semi-) leptonic decays of D_s (by Huijing LI)
- Branching Fraction Measurement of $D_{(s)}$
Hadronic decays
- Status of charm baryon physics
- Summary

BESIII experiment

Nucl. Instr. Meth. A 614, 345 (2010)

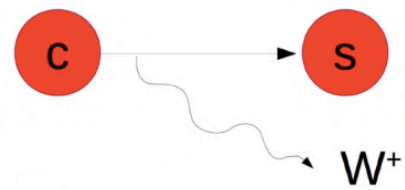
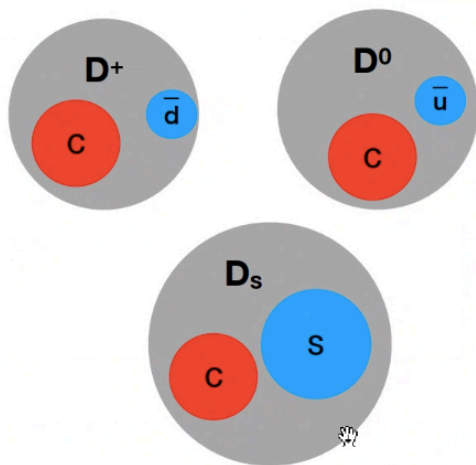


Beam energy: 1.0-2.35 GeV; E_{cms} now up to $\sqrt{s} \sim 4.9$ GeV
Design luminosity: $1 \times 10^{33} / \text{cm}^2 / \text{s}$ @ $\psi(3770)$
Achieved luminosity: $1.01 \times 10^{33} / \text{cm}^2 / \text{s}$ (2016)
Crossing angle: 11 mrad

MDC: $\sigma_p/P = 0.5\%$ @ 1 GeV, $\sigma_{r\phi} \sim 115 \mu\text{m}$, $\sigma_{dE/dx} = 5\%$
EMC: Energy: 2.5% @ 1 GeV
TOF: Barrel: 68 ps
Endcap: 100 \rightarrow 60 ps (update to MRPC)

From Dr. Xiaoshuai Qin's talk on QCD20

Physics of $D_{(s)}$ meson



Cabibbo-favored decay

As the lightest and most common mesons containing a single charm quark, D mesons can only decay through the weak interaction and plays a key role in our understanding of charm quarks.

Beam constrained Mass (M_{bc})

$$M_{bc} \equiv \sqrt{E_{beam}^2 - \left(\sum_i \vec{p}_i\right)^2} = \sqrt{E_{beam}^2 - p_D^2}$$

$$\delta M_{bc} \equiv \frac{E_{beam}}{M_{bc}} \delta E_{beam} \oplus \frac{p_D}{M_{bc}} \delta p_D$$

\vec{p}_i : measured momentum of daughter particle

p_D : measured momentum of D meson

M_{bc} peaks at D meson mass:
momentum conservation

Note: $\frac{p_D}{M_{bc}} = \frac{1}{7} \frac{E_{beam}}{M_{bc}}$

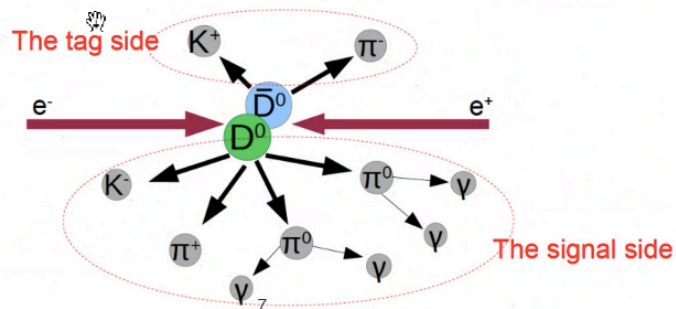
Most uncertainty comes from beam energy smearing.

BESIII Data Taken near DD^{bar} Threshold

- BEPCII collider: $e^+e^- \rightarrow \psi(3770) \rightarrow DD^{\text{bar}}$
- 2.9 fb^{-1} dataset at $\psi(3770)$ resonance
 - $M_{D^0} = 1864.84 \text{ MeV}$ $M_{D^+} = 1869.62 \text{ MeV}$
 - $2M_{D^0} = 3729.68 \text{ MeV}$ $2M_{D^+} = 3739.24 \text{ MeV}$
- 3.19 fb^{-1} dataset at $E_{\text{cm}} 4.178 \text{ GeV}$
 - D_s are produced mostly via $e^+e^- \rightarrow D_s D_s^*$
- New XYZ dataset at $E_{\text{cm}} 4.19 - 4.23 \text{ GeV}$ (about .8x of 4180 data)
- Advantages of DD^{bar} pair production near threshold
 - The DD^{bar} events are clean; not enough energy for even one additional pion
 - Tagging reduces background from light-quark “continuum” and other charm final states
 - Double tag technique can provide access to absolute BFs
 - Many systematic uncertainties cancel with tagging technique

DTag Technique

- There are two types of samples used in the Dtag technique: single tag (ST) and double tag (DT).
- Single tag: only one D meson is reconstructed through a chosen hadronic decay.
- Double tag: both D and \bar{D} are reconstructed,
 - the D reconstructed through **the studied hadronic decay** is called **“the signal side”**
 - the \bar{D} reconstructed through **well-known and clean hadronic decay** modes is called **“the tag side”**.
- (Charge-conjugate states are implied throughout this talk.)



Branching Fraction and Tagging

- Single tag (ST)

$$N_{\text{tag}}^{\text{ST}} = 2N_{D^0\bar{D}^0} \mathcal{B}_{\text{tag}} \epsilon_{\text{tag}}$$

- Double tag (DT)

$$N_{\text{tag,sig}}^{\text{DT}} = 2N_{D^0\bar{D}^0} \mathcal{B}_{\text{tag}} \mathcal{B}_{\text{sig}} \epsilon_{\text{tag,sig}}$$

$\epsilon_{\text{tag,sig}} \approx \epsilon_{\text{tag}} \epsilon_{\text{sig}}$ (factorization)

where $N_{D^0\bar{D}^0}$ is the total number of produced $D^0\bar{D}^0$ pairs, $\mathcal{B}_{\text{tag(sig)}}$ is the branching fraction of the tag (signal) side, and the ϵ are the corresponding efficiencies.

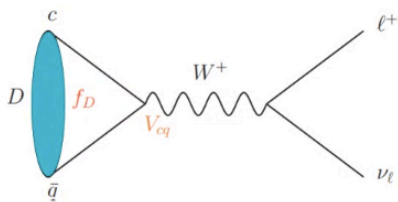
→
$$\mathcal{B}_{\text{sig}} = \frac{N_{\text{tag,sig}}^{\text{DT}}}{N_{\text{tag}}^{\text{ST}}} \frac{\epsilon_{\text{tag}}}{\epsilon_{\text{tag,sig}}}$$

$N_{D^0\bar{D}^0}$, \mathcal{B}_{tag} are canceled.
 ϵ_{tag} is approximately canceled due to factorization

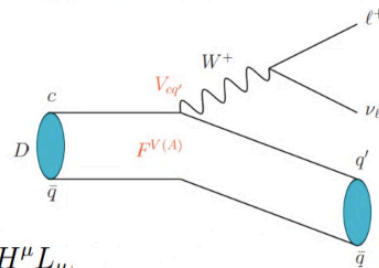
This is the basic idea for branching fraction.
Equations used in analysis vary case by case.

Introduction

$D_{(s)}$ pure leptonic decay



$D_{(s)}$ semi-leptonic decay



$$\mathcal{M} \propto |V_{cs(d)}| H^\mu L_\mu$$

$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu_l) \propto |f_{D_{(s)}^+}|^2 \cdot |V_{cd(s)}|^2$$

$$\Gamma(D_{(s)} \rightarrow P l^+ \nu_l) \propto |f_+(q^2)|^2 \cdot |V_{cd(s)}|^2$$

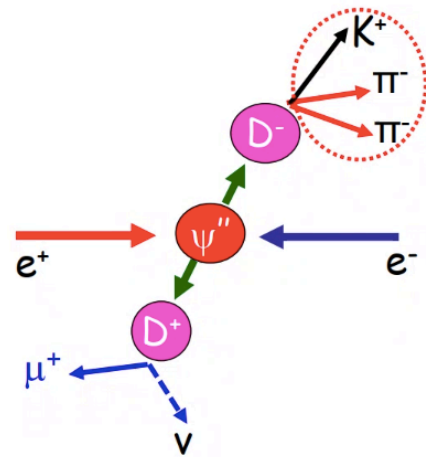
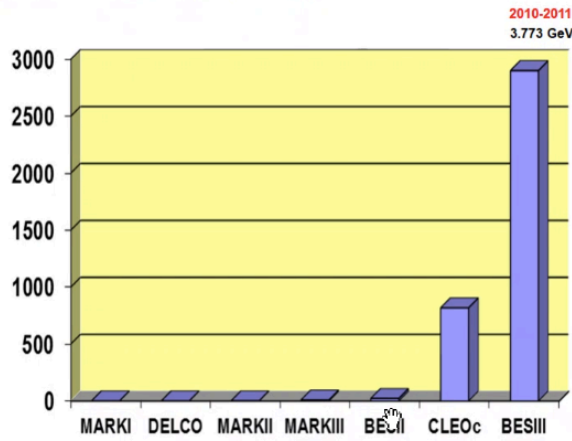
Decay constant $f_{D_{(s)}^+}$, form factor $f_+(q^2)$: Calibrate Lattice QCD

CKM matrix element $|V_{cd(s)}|$: Test the unitarity of CKM matrix and search for NP beyond SM

Lepton flavor universality test in charm sector

Introduction

$D^{0(+)}$ samples at $\psi(3770)$



$$N_{ST}^i = 2 \times N_{D\bar{D}} \times B_{ST}^i \times \epsilon_{ST}^i$$

$$N_{DT}^i = 2 \times N_{D\bar{D}} \times B_{ST}^i \times B_{sig} \times \epsilon_{ST vs. sig}^i$$

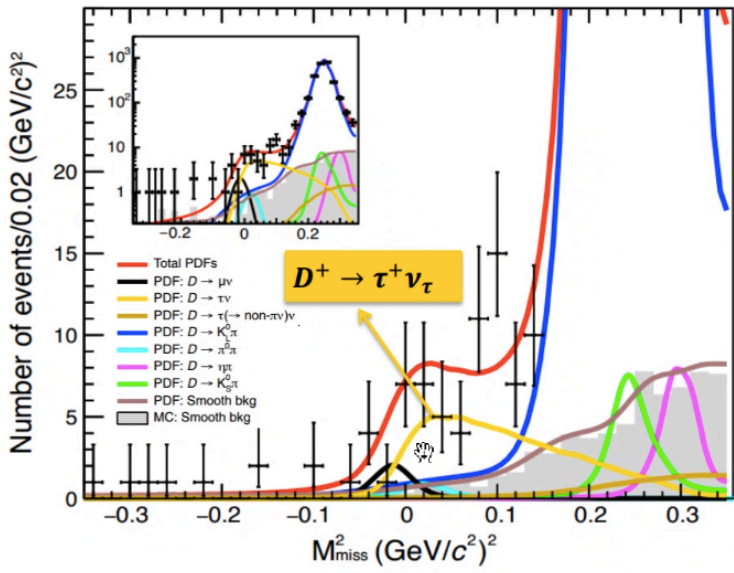
$$B_{sig} = \frac{N_{DT}^{tot}}{N_{ST}^{tot} \times \epsilon_{sig}}$$

$$\epsilon_{sig} = \frac{\sum_{i=1}^N (N_{ST}^i \times \epsilon_{ST vs. sig}^i / \epsilon_{ST}^i)}{\sum_{i=1}^N N_{ST}^i}$$

$$U_{miss} = E_{miss} - |\vec{p}_{miss}|$$

$$M_{miss}^2 = E_{miss}^2 - |\vec{p}_{miss}|^2$$

$D^+ \rightarrow \tau^+ \nu_\tau$
Phys. Rev. Lett. **123**, 211802 (2019)



137 ± 27 signal events

First observation with a significance of 5.1σ.

$$B(D^+ \rightarrow \tau^+ \nu_\tau) = (1.20 \pm 0.24 \pm 0.12) \times 10^{-3}$$

$$R_D \equiv \frac{\Gamma(D^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D^+ \rightarrow \mu^+ \nu_\mu)} = 3.21 \pm 0.77$$

↕ consistent

$$|V_{cd}| = 0.237 \pm 0.024_{\text{stat.}} \pm 0.012_{\text{syst.}} \pm 0.001_{\text{ex-syst}}$$

$$f_{D^+} = 224.5 \pm 22.8_{\text{stat.}} \pm 11.3_{\text{syst.}} \pm 0.9_{\text{ex-syst.}} \text{ MeV}$$

2020/11/07 K.Liu

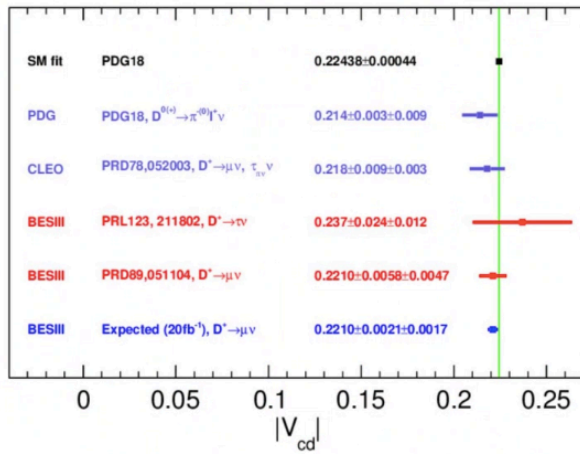
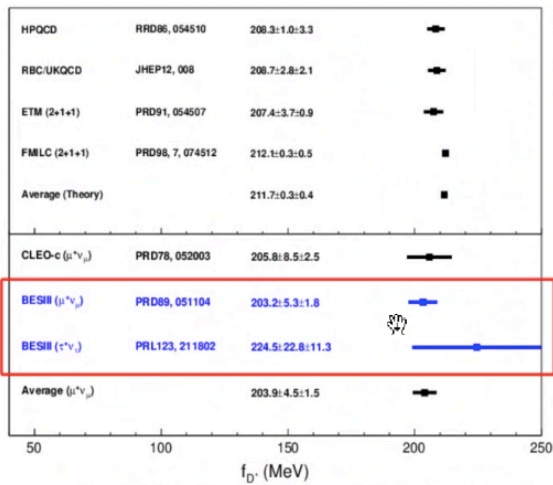
SM:

$$R_{\tau/\mu} = \frac{\Gamma(D^+ \rightarrow \tau^+ \nu_\tau)}{\Gamma(D^+ \rightarrow \mu^+ \nu_\mu)} = \frac{m_\tau^2 (1 - \frac{m_\tau^2}{M_{D^+}^2})^2}{m_\mu^2 (1 - \frac{m_\mu^2}{M_{D^+}^2})^2} = 2.7$$

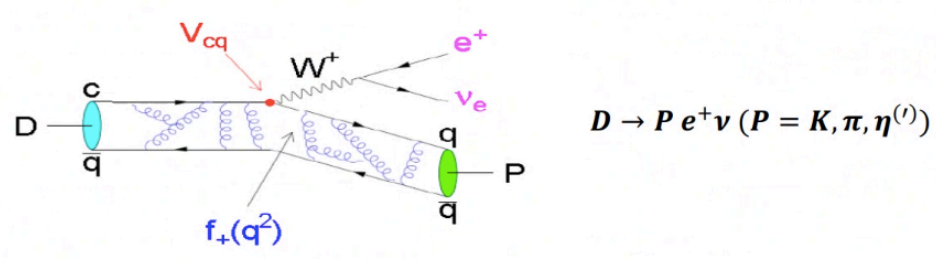
Comparison of f_{D^+} and $|V_{cd}|$

Input: $|V_{cd}| = 0.22438 \pm 0.00044$
 PDG2018 from CKM unitarity

Input: $f_{D^+} = 212.3 \pm 0.6$ MeV
 LQCD average



Semi-leptonic decay



$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 p^3}{24\pi^3} |f_+(q^2)|^2 |V_{cd(s)}|^2 \quad (X = 1 \text{ for } K^-, \pi^-, \bar{K}^0, \eta^{(\prime)}; X = \frac{1}{2} \text{ for } \pi^0)$$

- Single pole form $\frac{f_+(0)}{1 - q^2/M_{pole}^2}$

- Modified pole model

$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/M_{pole}^2}$$

$$f_+(q^2) = \frac{f_+(0)}{\left(1 - \frac{q^2}{M_{pole}^2}\right) \left(1 - \alpha \frac{q^2}{M_{pole}^2}\right)}$$

- ISGW2 model

- Series expansion model

$$f_+(q^2) = f_+(q_{max}^2) \left(1 + \frac{r^2}{12} (q_{max}^2 - q^2)\right)^{-2}$$

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

$D^{0(+)} \rightarrow \pi^{-(0)} \mu^+ \nu_\mu$
Phys. Rev. Lett. **121**, 171803(2019)

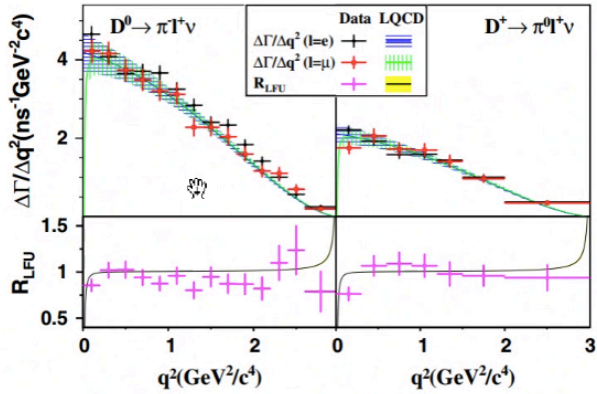
SM expectation: **0.985 ± 0.002** [*Eur. Phys. J.* C78,501(2018)]

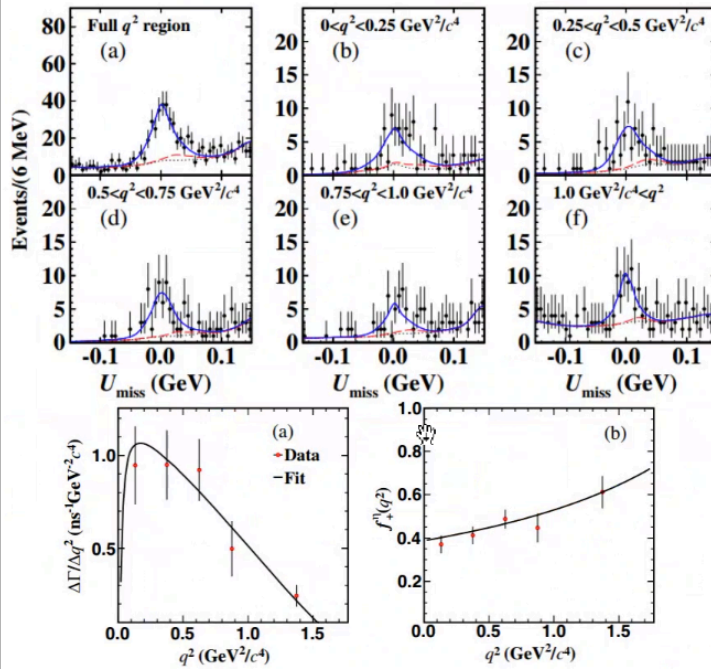
$$R_{LFU}^{\pi^-} = \frac{\Gamma(D^0 \rightarrow \pi^- \mu^+ \nu_\mu)}{\Gamma(D^0 \rightarrow \pi^- e^+ \nu_e)} = 0.922 \pm 0.030 \pm 0.022$$

1.7 σ consistent

$$R_{LFU}^{\pi^0} = \frac{\Gamma(D^+ \rightarrow \pi^0 \mu^+ \nu_\mu)}{\Gamma(D^+ \rightarrow \pi^0 e^+ \nu_e)} = 0.964 \pm 0.037 \pm 0.026$$

0.5 σ consistent



$D^+ \rightarrow \eta \mu^+ \nu_\mu$
Phys. Rev. Lett. 124, 231801(2020)


$$\mathcal{B}(D^+ \rightarrow \eta \mu^+ \nu_\mu) = (10.4 \pm 1.0 \pm 0.5) \times 10^{-4}$$

$$f_+^\eta(0)|V_{cd}| = 0.087 \pm 0.008 \pm 0.002$$

$$f_+^\eta(0) = 0.39 \pm 0.04 \pm 0.01$$

$$|V_{cd}| = 0.242 \pm 0.022 \pm 0.006 \pm 0.033$$

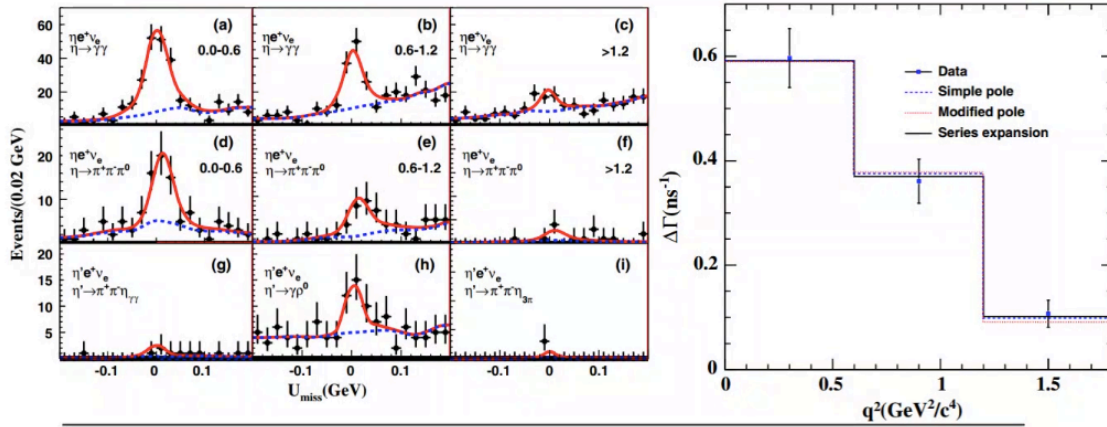
$$R = \frac{\mathcal{B}(D^+ \rightarrow \eta \mu^+ \nu_\mu)}{\mathcal{B}(D^+ \rightarrow \eta e^+ \nu_e)_{\text{PDG}}} = 0.91 \pm 0.13$$

SM(0.97-1.00)

 no LFU violation within
current sensitivity

 Experimental confirmation
for the first time since it was
predicted in 30 years ago.
Phys. Rev. D 39, 799 (1989).

$D^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$
Phys. Rev. D 97, 092009(2018)

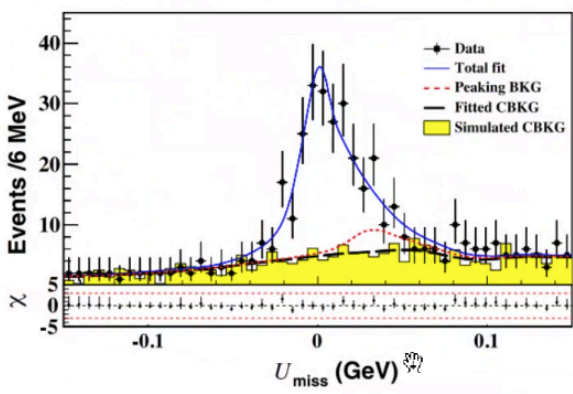


| Fit parameters | Simple pole | Modified pole | Series expansion |
|-----------------------------------|--------------------------|--------------------------|---------------------------|
| $f_+(0) V_{cd} (\times 10^{-2})$ | $8.15 \pm 0.45 \pm 0.18$ | $8.24 \pm 0.51 \pm 0.22$ | $7.86 \pm 0.64 \pm 0.21$ |
| Shape parameter | $1.73 \pm 0.17 \pm 0.03$ | $0.50 \pm 0.54 \pm 0.08$ | $-7.33 \pm 1.69 \pm 0.40$ |
| ρ | 0.80 | -0.85 | 0.90 |
| χ^2/ndf | 0.1/(3-2) | 0.3/(3-2) | 0.5/(3-2) |

$\eta - \eta'$ mixing angle ϕ_P can be determined

$$\cot^4 \phi_P = \frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu_e) / \Gamma(D_s^+ \rightarrow \eta e^+ \nu_e)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu_e) / \Gamma(D^+ \rightarrow \eta e^+ \nu_e)} \quad \Phi_P = (40.1 \pm 2.1 \pm 0.7)^\circ$$

$D^+ \rightarrow \omega \mu^+ \nu_\mu$
Phys. Rev. D 101, 072005(2020)



$$\mathcal{B}(D^+ \rightarrow \omega \mu^+ \nu_\mu) = (17.7 \pm 1.8 \pm 1.1) \times 10^{-4}$$

This BF is consistent with theoretical calculation (LFQM, CCQM, and LCSR methods).

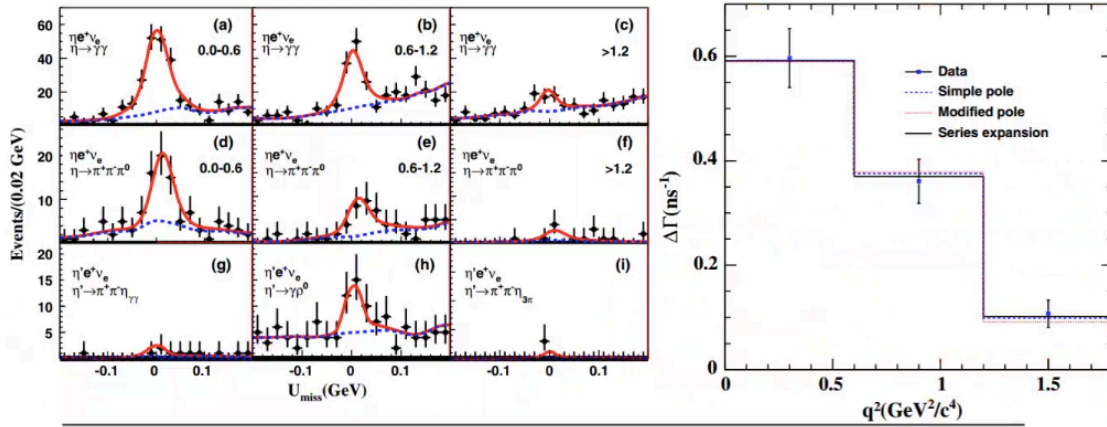
$$R = \frac{\mathcal{B}(D^+ \rightarrow \omega \mu^+ \nu_\mu)}{\mathcal{B}(D^+ \rightarrow \omega e^+ \nu_e)_{\text{PDG}}} = 1.05 \pm 0.14$$

SM(0.93-0.99)

no LFU violation within current statistics

Experimental confirmation for the first time since it was predicted in 30 years ago. *Phys. Rev. D 39, 799 (1989)*.

$D^+ \rightarrow \eta^{(\prime)} e^+ \nu_e$
Phys. Rev. D 97, 092009(2018)

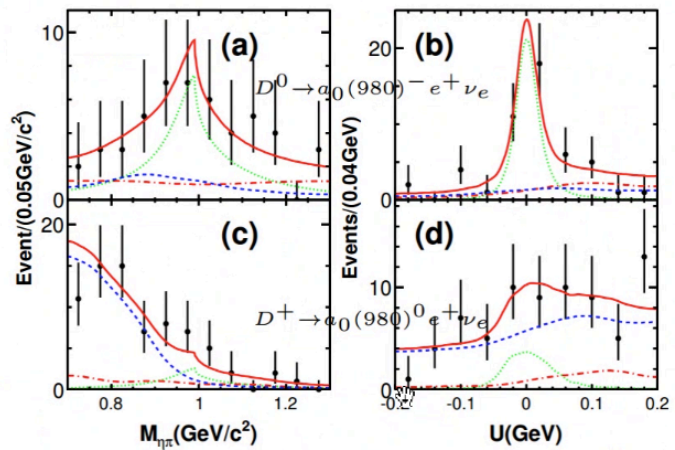


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| Shape parameter | $1.73 \pm 0.17 \pm 0.03$ | $0.50 \pm 0.54 \pm 0.08$ | $-7.33 \pm 1.69 \pm 0.40$ |
| ρ | 0.80 | -0.85 | 0.90 |
| χ^2/ndf | 0.1/(3-2) | 0.3/(3-2) | 0.5/(3-2) |

$\eta - \eta'$ mixing angle ϕ_P can be determined

$$\cot^4 \phi_P = \frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu_e) / \Gamma(D_s^+ \rightarrow \eta e^+ \nu_e)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu_e) / \Gamma(D^+ \rightarrow \eta e^+ \nu_e)} \quad \Phi_P = (40.1 \pm 2.1 \pm 0.7)^\circ$$

$D^{0/+} \rightarrow a_0(980)^{-/0} e^+ \nu_e$
***Phys. Rev. Lett.* 121, 081802(2018)**



A model-independent way to study the nature of light scalar mesons proposed by PRD82(2016)034016

$$R = \frac{\mathcal{B}(D^+ \rightarrow f_0(980) e^+ \nu_e) + \mathcal{B}(D^+ \rightarrow f_0(500) e^+ \nu_e)}{\mathcal{B}(D^+ \rightarrow a_0(980)^0 e^+ \nu_e)}$$

$R = 1.0 \pm 0.3$ for two-quark description;
 $R = 3.0 \pm 0.9$ for tetraquark description.

We have $R > 2.7$ @90% C.L. at BESIII
 Which favors the tetraquark description.

| Decay | BF ($\times 10^{-4}$) | Significance |
|---|---|--------------|
| $D^0 \rightarrow a_0(980)^- e^+ \nu_e, a_0(980)^- \rightarrow \eta \pi^-$ | $1.33^{+0.33}_{-0.29} \pm 0.09$ | 6.4σ |
| $D^+ \rightarrow a_0(980)^0 e^+ \nu_e, a_0(980)^0 \rightarrow \eta \pi^0$ | $1.66^{+0.81}_{-0.66} \pm 0.11$ < 3.0 (90% C.L.) | 2.9σ |

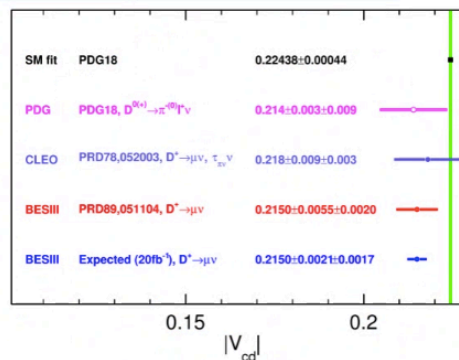
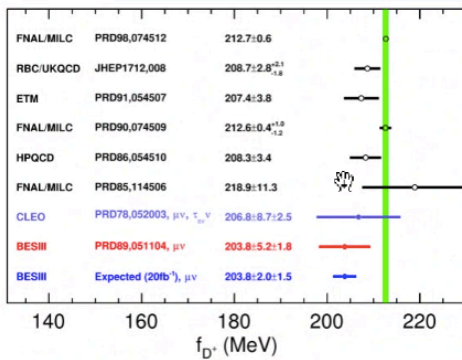
Prospect

From White Paper (Chin. Phys. C 44, 040001 (2020))

With 20 fb⁻¹ of data set at 3.773 GeV in the coming two years

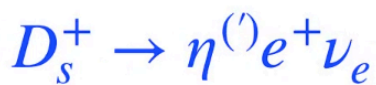
Leptonic Decay

| | 2.93 fb ⁻¹ | 20 fb ⁻¹ |
|-----------------|-----------------------|---------------------|
| f_{D^+} | 2.6% | 1.0% |
| $ V_{cd} $ | 2.5% | 1.0% |
| R_{D^+} (LFU) | 19% | 8% |



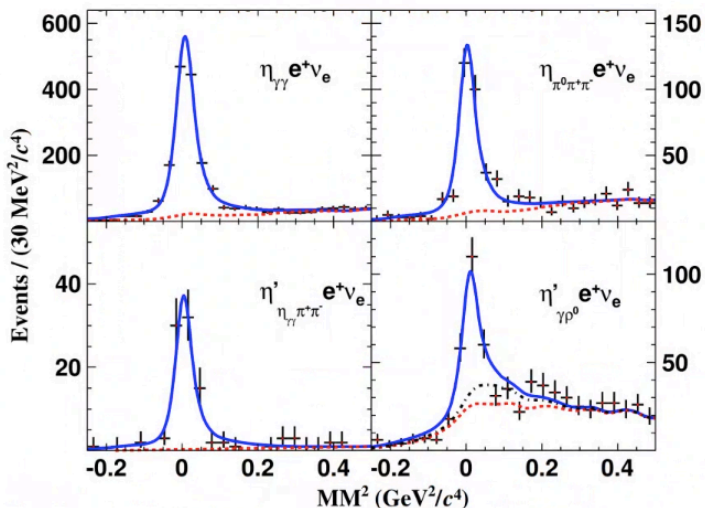
BESIII is expected to provide unique data in the next decade to improve the knowledge of f_{D^+} and $|V_{cd}|$ and test LFU in $D^+ \rightarrow l^+ \nu_l$ decays.

(Semi-) leptonic decays of D_s



PRL 122 (2019) 121801

A simultaneous unbinned maximum likelihood fit



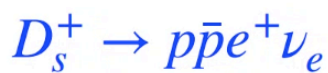
Two modes: constrained to be the same branching fraction after considering the different efficiencies and subdecay branching fractions.

Non-peaking background

$D_s^+ \rightarrow \phi e^+ \nu_e$

$$\mathcal{B}_{D_s^+ \rightarrow \eta e^+ \nu_e} = (2.323 \pm 0.063_{\text{stat}} \pm 0.063_{\text{syst}}) \%$$

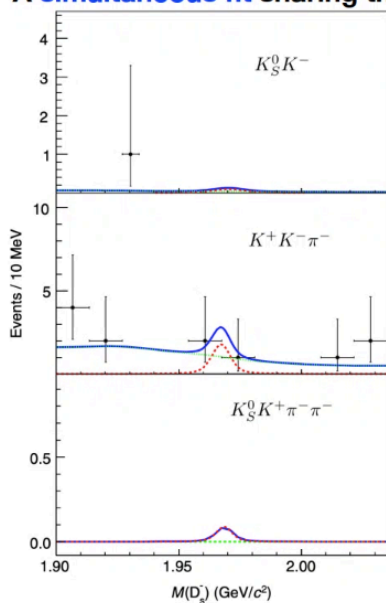
$$\mathcal{B}_{D_s^+ \rightarrow \eta' e^+ \nu_e} = (0.824 \pm 0.073_{\text{stat}} \pm 0.027_{\text{syst}}) \%$$



PRD 100 (2019) 112008

- It is useful input in understanding the baryonic transition of D_s^+ mesons;
- Search for the near-threshold enhancement in $p\bar{p}$ system.

A simultaneous fit sharing the same branching fraction



$$N_{\text{sig}}^1 = 0.3^{+0.4}_{-0.3}$$

Statistical significance: 1.2σ

$$\mathcal{B}_{D_s^+ \rightarrow p\bar{p}e^+\nu_e} = (0.50^{+0.63}_{-0.44}) \times 10^{-4}$$

$$N_{\text{sig}}^2 = 1.4^{+1.8}_{-1.3}$$

Upper limit @ 90% CL.:

$$\mathcal{B}(D_s^+ \rightarrow p\bar{p}e^+\nu_e) < 2.0 \times 10^{-4}$$

$$N_{\text{sig}}^3 = 0.1 \pm 0.1$$

Branching fraction measurements of charmed meson hadronic decays

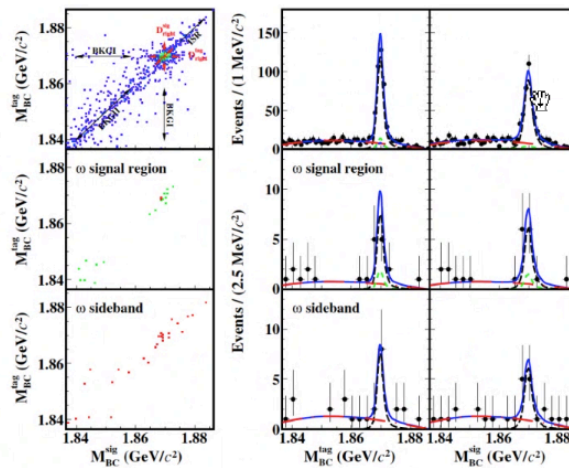
Observation of the DCS decay $D^+ \rightarrow K^+ \pi^+ \pi^- \pi^0$

Phys. Rev. Lett. 125, 141802 (2020)

| Decay mode | N_{DT} | $\mathcal{B}_{sig} (\times 10^{-3})$ |
|---|---------------------|--------------------------------------|
| $D^\pm \rightarrow K^\pm \pi^\pm \pi^\mp \pi^0$ | 350 ± 22 | 1.21 ± 0.08 |
| $D^\pm \rightarrow K^\pm \omega$ | $9.2^{+4.0}_{-3.4}$ | $(5.7^{+2.5}_{-2.1}) \times 10^{-2}$ |
| $D^+ \rightarrow K^+ \pi^+ \pi^- \pi^0$ | 181 ± 15 | 1.25 ± 0.11 |
| $D^- \rightarrow K^- \pi^- \pi^+ \pi^0$ | 165 ± 15 | 1.16 ± 0.11 |

subtracting the η, ω, ϕ

$$B_{DCS} = (1.13 \pm 0.08 \pm 0.03) \times 10^{-3}$$



$$B_{DCS}/B_{CF} = (1.81 \pm 0.15\%) = (6.28 \pm 0.52)\tan^4 \theta_C$$

Significantly larger than (0.21~0.58%) from other DCS decays
Possible sizable isospin symmetry violation effects

Measurements of SCS

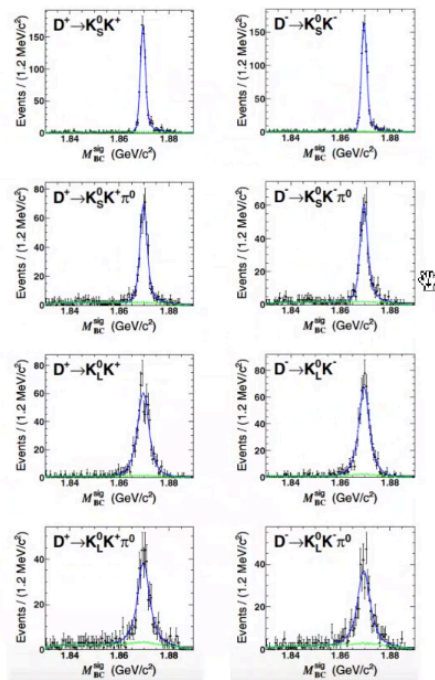


Phys. Rev. D 99, 032002 (2019)

To select the candidates of K_L , the momentum direction of the K_L particle is inferred by the position of a shower in the EMC, and a kinematic fit imposing momentum and energy conservation for the observed particles and a missing K_L particle is performed to select the signal.

First measurements of three SCS D decays

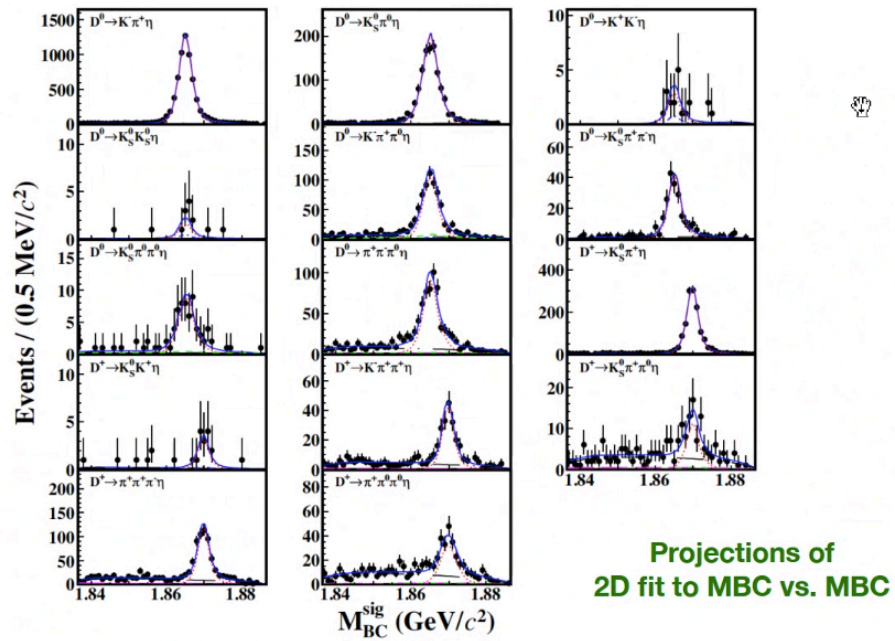
CP Asymmetry is also examined, but no evidence is observed



| Signal mode | $\mathcal{B}(D^+) (\times 10^{-3})$ | $\mathcal{B}(D^-) (\times 10^{-3})$ | $\bar{\mathcal{B}} (\times 10^{-3})$ | $\mathcal{B} \text{ (PDG)} (\times 10^{-3})$ | $\mathcal{A}_{CP} (\%)$ |
|---------------------|-------------------------------------|-------------------------------------|--------------------------------------|--|-------------------------|
| $K_S^0 K^\pm$ | $2.96 \pm 0.11 \pm 0.08$ | $3.07 \pm 0.12 \pm 0.08$ | $3.02 \pm 0.09 \pm 0.08$ | 2.95 ± 0.15 | $-1.8 \pm 2.7 \pm 1.6$ |
| $K_S^0 K^\pm \pi^0$ | $5.14 \pm 0.27 \pm 0.24$ | $5.00 \pm 0.26 \pm 0.22$ | $5.07 \pm 0.19 \pm 0.23$ | ... | $1.4 \pm 3.7 \pm 2.4$ |
| $K_L^0 K^\pm$ | $3.07 \pm 0.14 \pm 0.10$ | $3.34 \pm 0.15 \pm 0.11$ | $3.21 \pm 0.11 \pm 0.11$ | ... | $-4.2 \pm 3.2 \pm 1.2$ |
| $K_L^0 K^\pm \pi^0$ | $5.21 \pm 0.30 \pm 0.22$ | $5.27 \pm 0.30 \pm 0.22$ | $5.24 \pm 0.22 \pm 0.22$ | ... | $-0.6 \pm 4.1 \pm 1.7$ |

Measurements of 14 exclusive $D \rightarrow \eta X$ decays

Phys. Rev. Lett. 124, 241803 (2020)



Amplitude Analysis of charmed meson hadronic decays

Selected Results in D Decays

1. $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ PRD 95, 072010 (2017)
2. $D^0 \rightarrow K^- \pi^+ \pi^0 \pi^0$ PRD 99, 092008 (2019)
3. $D^+ \rightarrow K_s^0 \pi^+ \pi^+ \pi^-$ Phys. Rev. D 100, 072008 (2019)
4. $D^+ \rightarrow K^- \pi^+ e^+ \nu$ PRD 94, 032001 (2016)
5. $D^+ \rightarrow \pi^- \pi^+ e^+ \nu, D^0 \rightarrow \pi^- \pi^0 e^+ \nu$ PRL 122, 062991 (2019)

Amplitude analysis of $D \rightarrow K\pi\pi\pi$

- The measurement of the sub-modes in $D \rightarrow K\pi\pi\pi$ provides a window to study the decays $D \rightarrow AP$ and $D \rightarrow VV$ (A =axial-vector, V =vector), both of them are important in learning the CPV in charm decays but less effective experimental measurements.
- The knowledge of sub-modes can be widely used in many measurements:
 - Branching fraction measurement
 - Strong phase measurement
 - CKM unitary triangle measurement
- There are seven $D \rightarrow K\pi\pi\pi$ modes:
 $D^0 \rightarrow K^-\pi^+\pi^+\pi^-, K^-\pi^+\pi^0\pi^0, K_S^0\pi^+\pi^-\pi^0, K_S^0\pi^0\pi^0\pi^0$ and $D^+ \rightarrow K^-\pi^+\pi^+\pi^0, K_S^0\pi^+\pi^+\pi^-, K_S^0\pi^+\pi^0\pi^0$.
Previous measurements of sub-modes in $D^0 \rightarrow K^-\pi^+\pi^+\pi^-, K_S^0\pi^+\pi^-\pi^0$ and $D^+ \rightarrow K^-\pi^+\pi^+\pi^0, K_S^0\pi^+\pi^+\pi^-$ have been performed by Mark III and E691. Both measurements are affected by low statistics.

BESIII 粲物理的未来展望

高精度检验标准模型的电弱(EW)理论和量子色动力学(QCD)理论是粒子物理研究前沿。粲强子衰变携带丰富的强作用和弱作用信息，是检验标准模型的理想场所

BESIII实验独特优势： 阈值附近产生各种量子关联的粲强子对，高精度，低本底，全重建

- 开展中性粲介子量子关联特性的研究，精确测量相关不同末态的平均强相位差和 CP 本征态成分比例，为CKM矩阵的 γ/ϕ_3 相角的精确测量提供关键参数；
- 精确测量CKM矩阵元，检验CKM矩阵的幺正性，探索新的 CP 破坏来源
- 精确测量粲强子衰变常数和半轻衰变形状因子，与格点QCD理论计算值比较，探寻超出标准模型新现象
- 系统地研究粲强子的强子末态衰变，研究强子谱学和末态相互作用，检验夸克味对称性
- 研究粲强子衰变，高精度检验轻子普适性，寻找稀有或禁戒的衰变过程，精密检验标准模型、寻找超出标准模型的新物理