

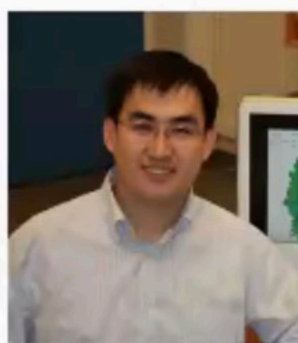
A Muon-Ion Collider (at BNL)

The future QCD frontier and path to a new energy frontier of $\mu^+\mu^-$ colliders
[arXiv:2107.02073](https://arxiv.org/abs/2107.02073)

Darin Acosta, Wei Li (Rice University)



Darin Acosta: Particle Physicist on CMS (Higgs, Standard Model physics and BSM searches etc.), funded by US DOE-HEP; Previously on CDF at the Tevatron, and on ZEUS at HERA ([ep collider](#))



Wei Li: Nuclear Physicist on CMS (high-energy nuclear collisions, QCD in extreme densities), funded by US DOE-NP; also on STAR (and previously PHOBOS) at RHIC (AA collider) and emerging collaborations at EIC ([ep/eA collider](#))

There are many examples of successful synergies between HEP and NP in CMS in physics measurements, detector design, operations and upgrades
In chatting about the future of each other's fields, we recognize further opportunities to collaborate...

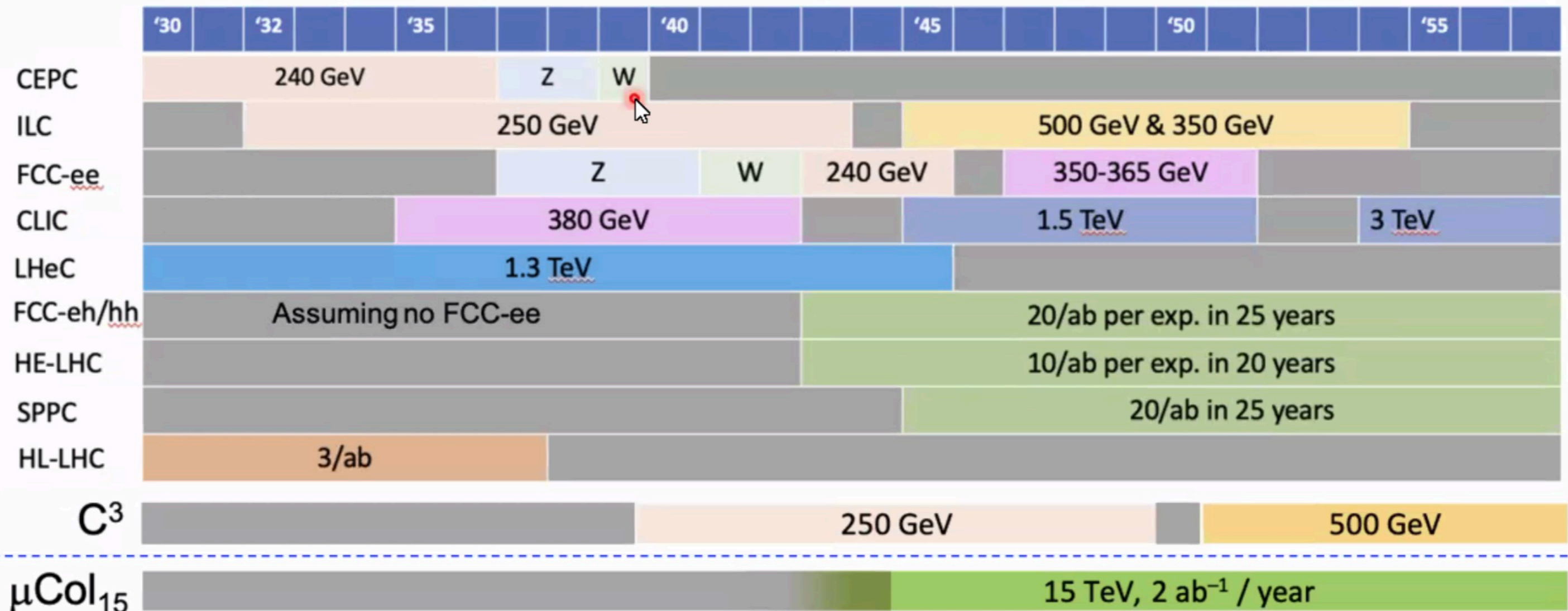
n.b. Neither of us is an accelerator expert...

Future of High Energy Physics Energy Frontier



- Many options for Higgs factories and energy frontier machines
- What would be an optimal and realistic path forward?

S. Dasu



Growing interests in muon colliders!

An Energy Frontier Muon Collider

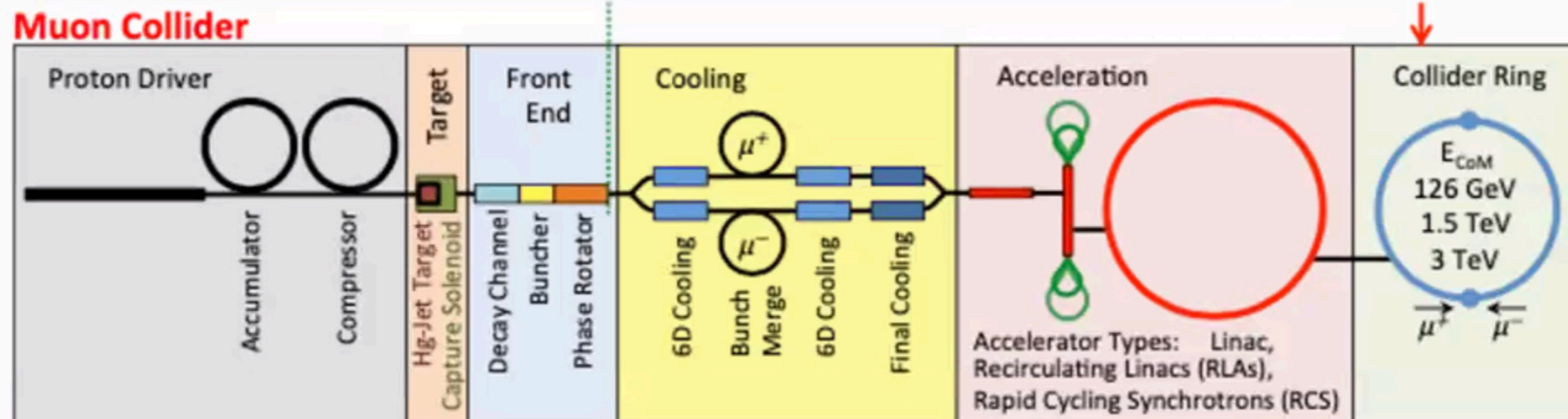
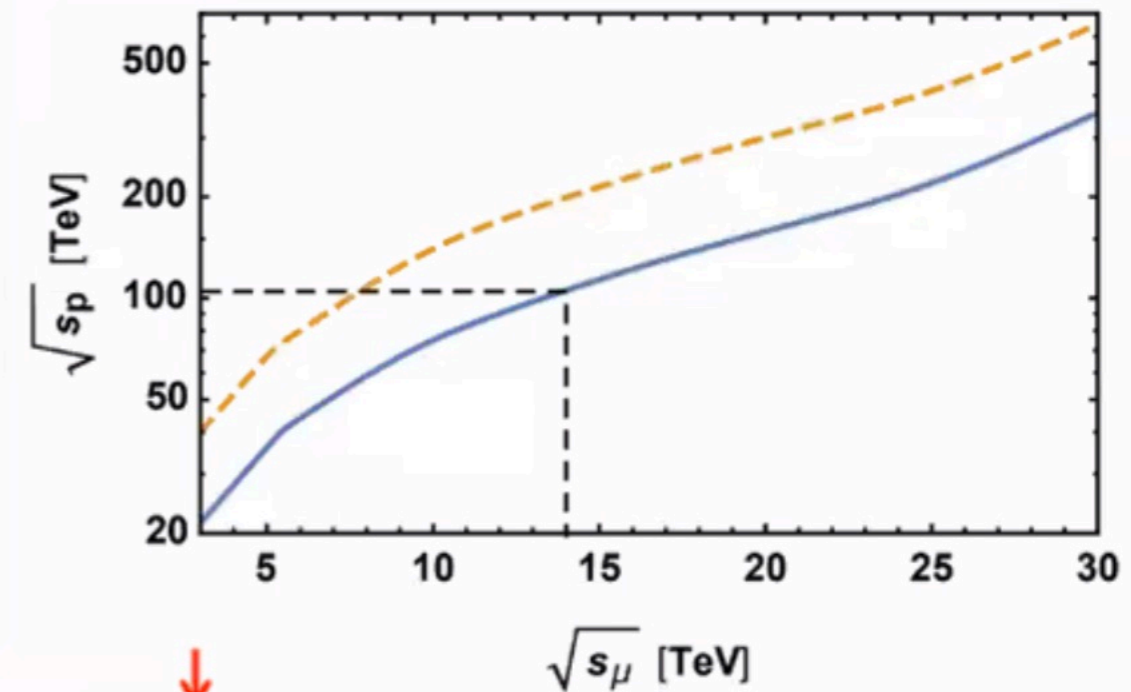


A more compact and innovative facility to incorporate the advantages of a high precision lepton collider and an energy frontier machine

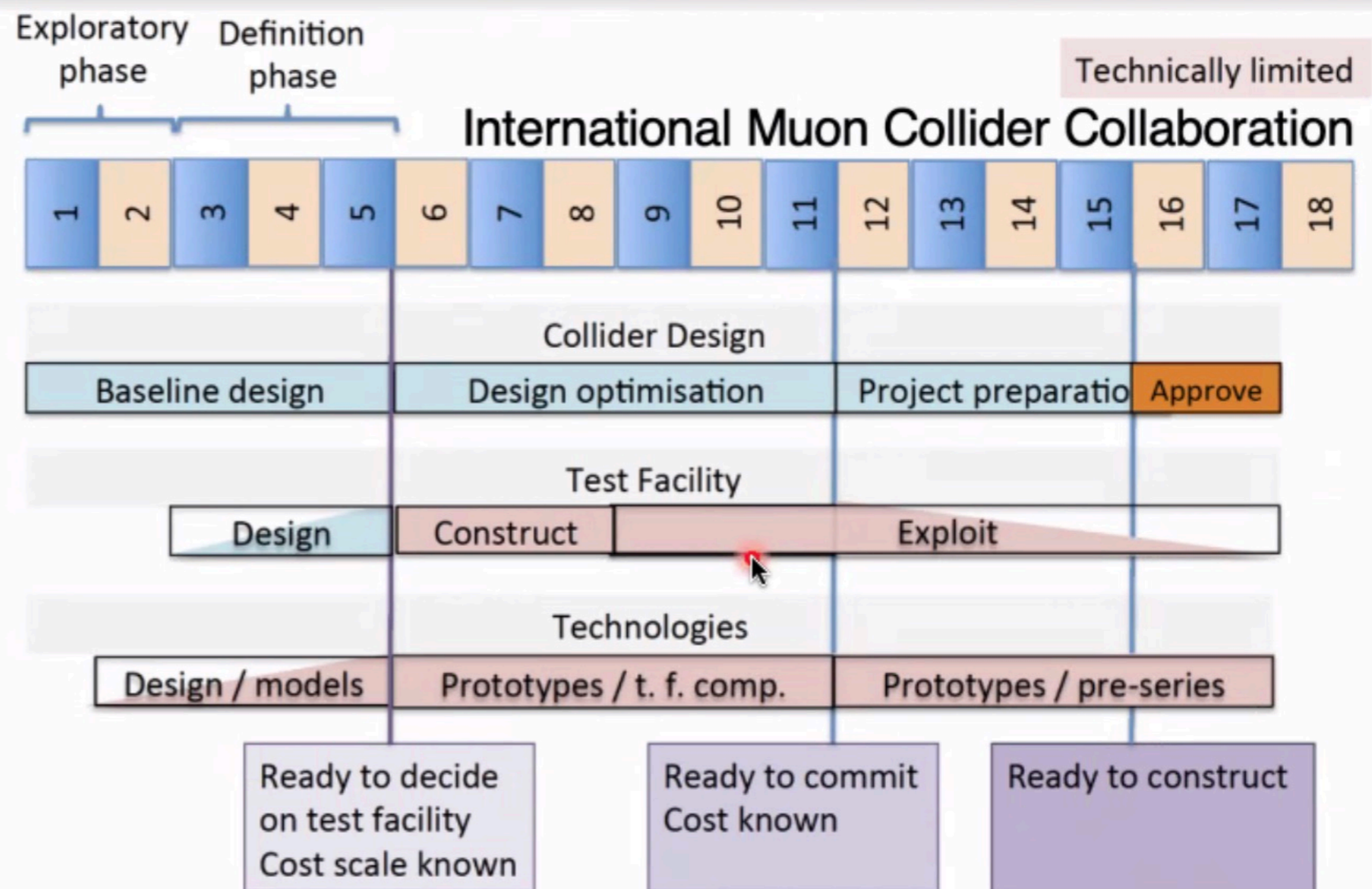
An $O(10)$ TeV muon collider has the equivalent mass reach to an $O(100)$ TeV proton collider

But much R&D still to do...

arXiv:1901.06150



Potential timeline of muon colliders



Physics potential along the way D. Schulte

Ultimate Beam Limits, April 6, 2021

arXiv:1901.06150

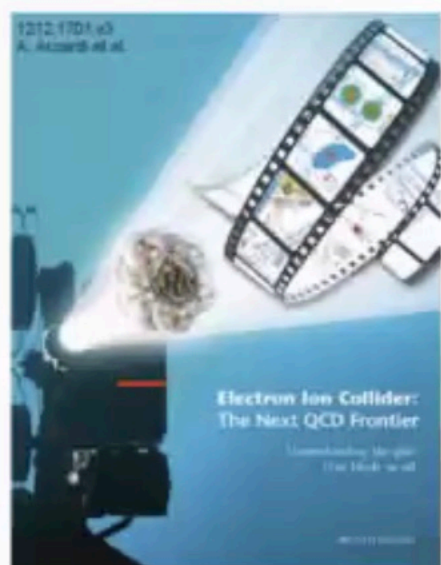
4

A vigorous and ambitious R&D program is needed to assess the feasibility of a tens-of-TeV's muon collider. Therefore it is important to investigate the physics potential of smaller-scale machines that might be built along the way as technology demonstrators. Starting from medium energy, the first option to be considered is a muon collider operating around the top production threshold (~ 400 GeV). This

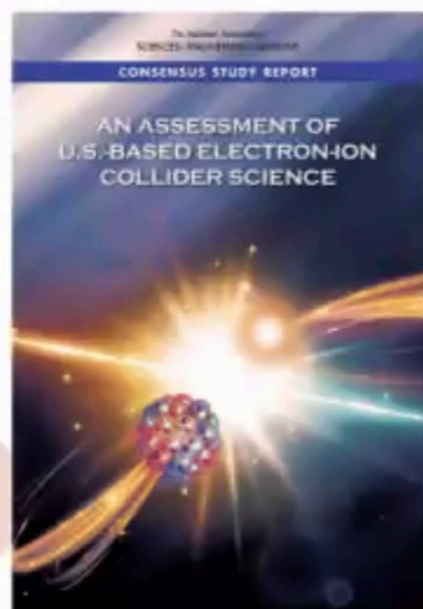
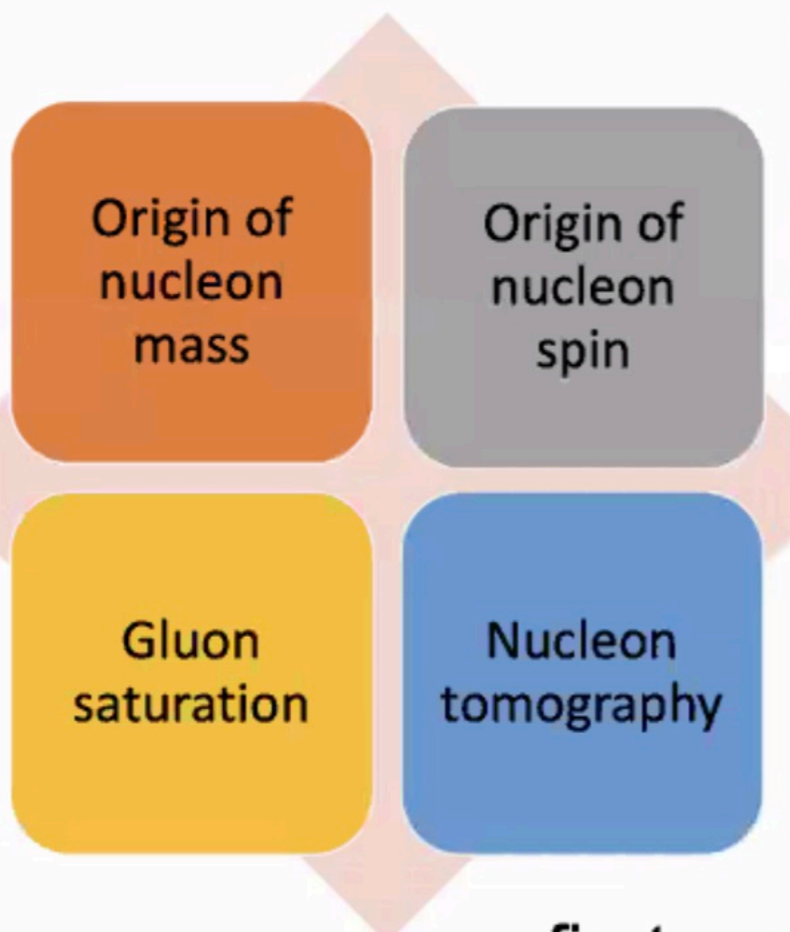
A demonstrator with compelling science is needed before going to O(10+) TeV



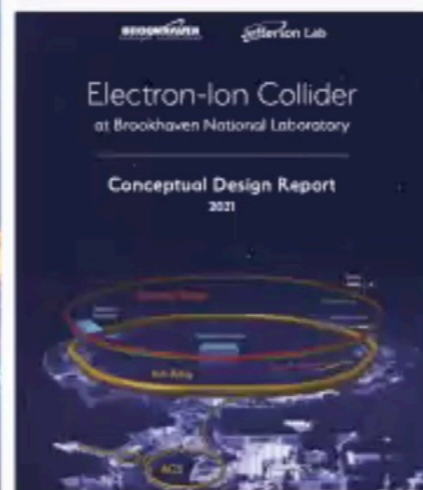
Electron-Ion Collider at BNL (2030-) – a new QCD frontier (CD-1, funded by DOE-NP)



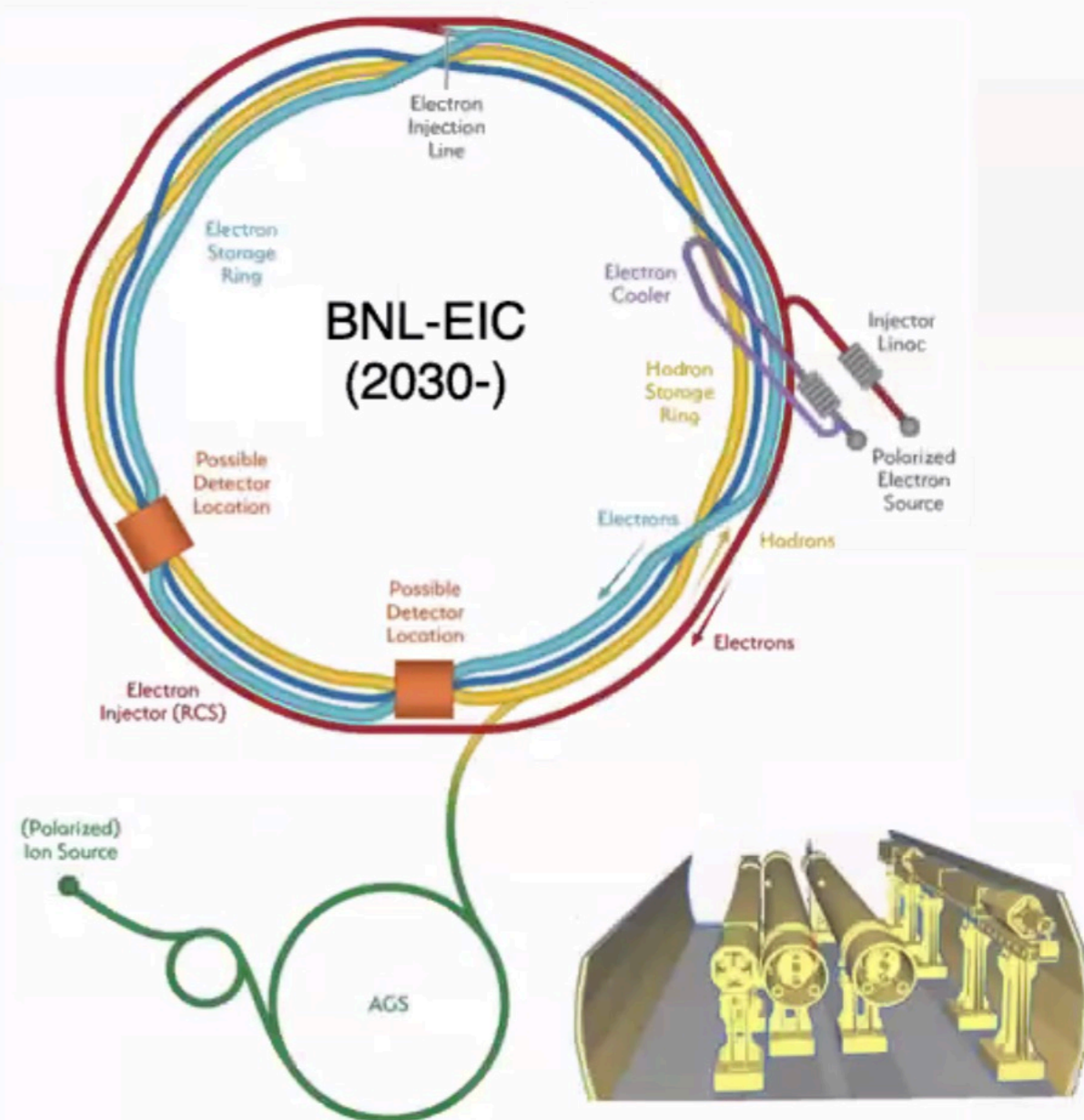
White paper
arXiv:1212.1701



NAS report
July 2018



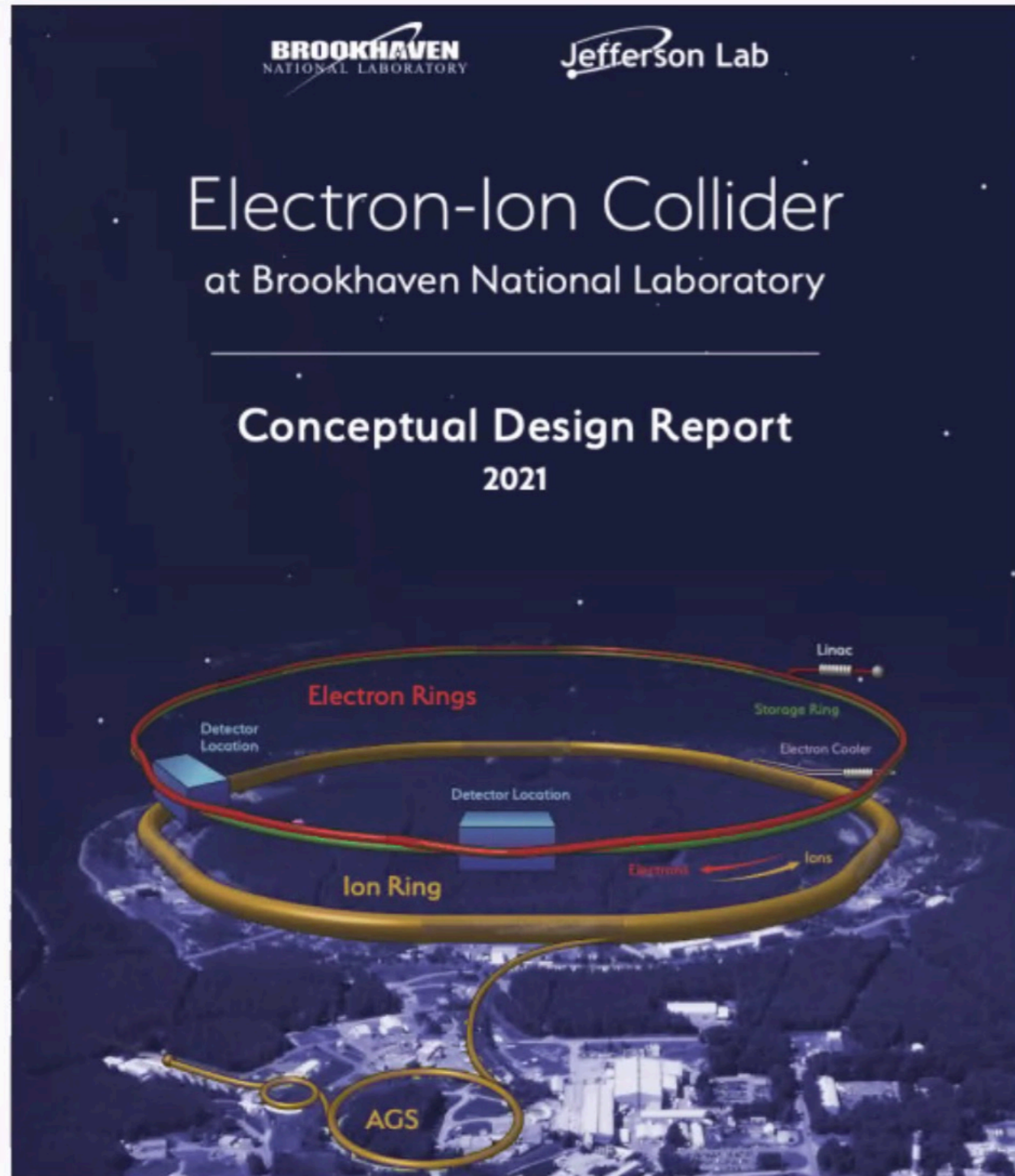
CDR 2021



first conceived in late 90s

ep, eA (any ion in periodic table) up to 140 GeV;
Polarized e, p, ^3He beams (70% polarization)

The Electron-Ion Collider (EIC)



[EIC Conceptual Design Report](#) just released and project approved

Salient points:

- Hadron beam energy up to 275 GeV (increase from RHIC)
- Electron beam energy up to 18 GeV
- $\sqrt{s} = 20 - 140$ GeV
- Luminosity $10^{33} - 10^{34}$ Hz/cm²
- Polarized electron, proton and ion beams (any)
- Design supports 2 detectors, only one in project scope

Physics goals:

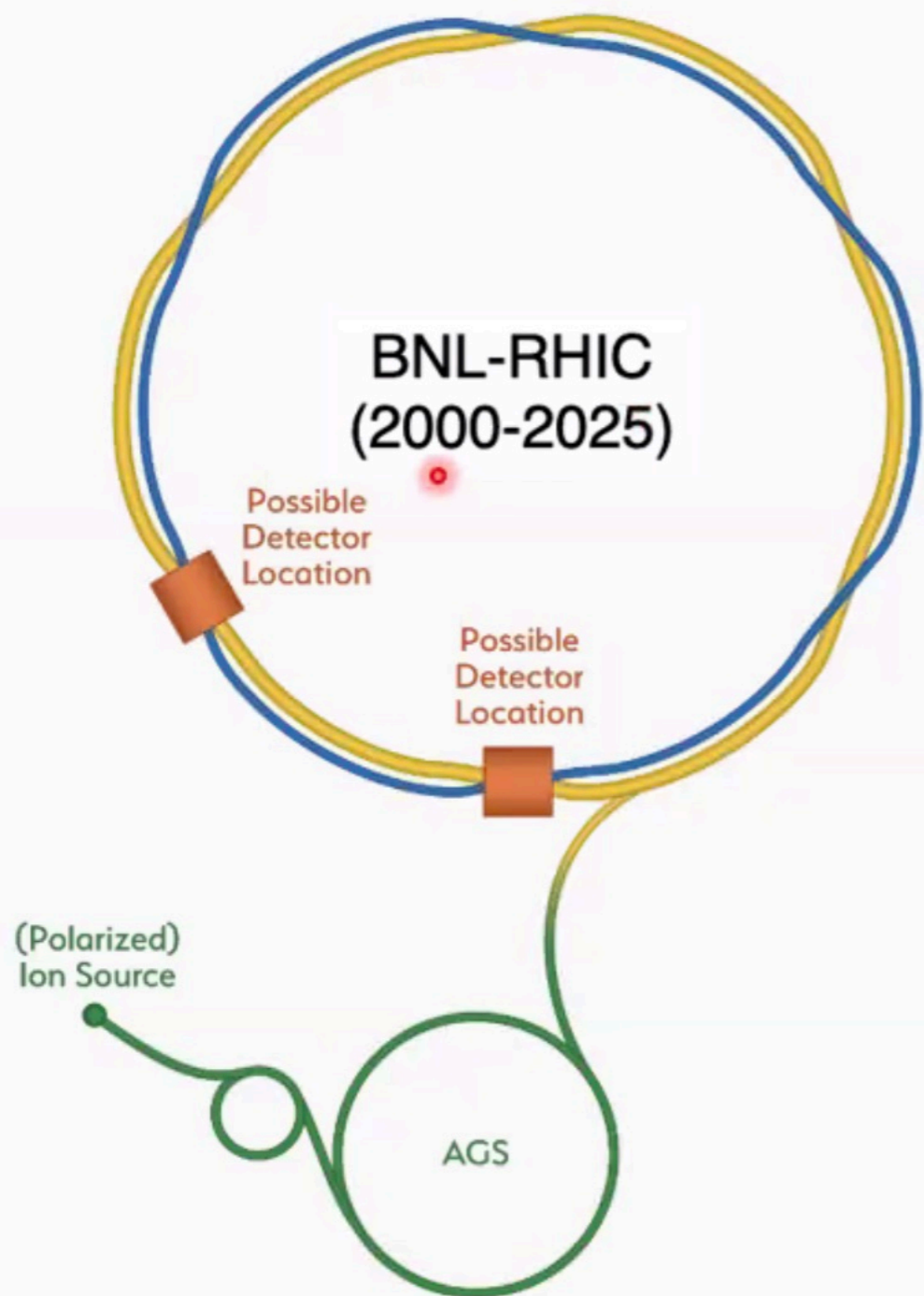
- ep and eN deep inelastic scattering
- Nucleon spin structure
- Gluon saturation scale (Q_s)

Electron-Ion Collider at BNL

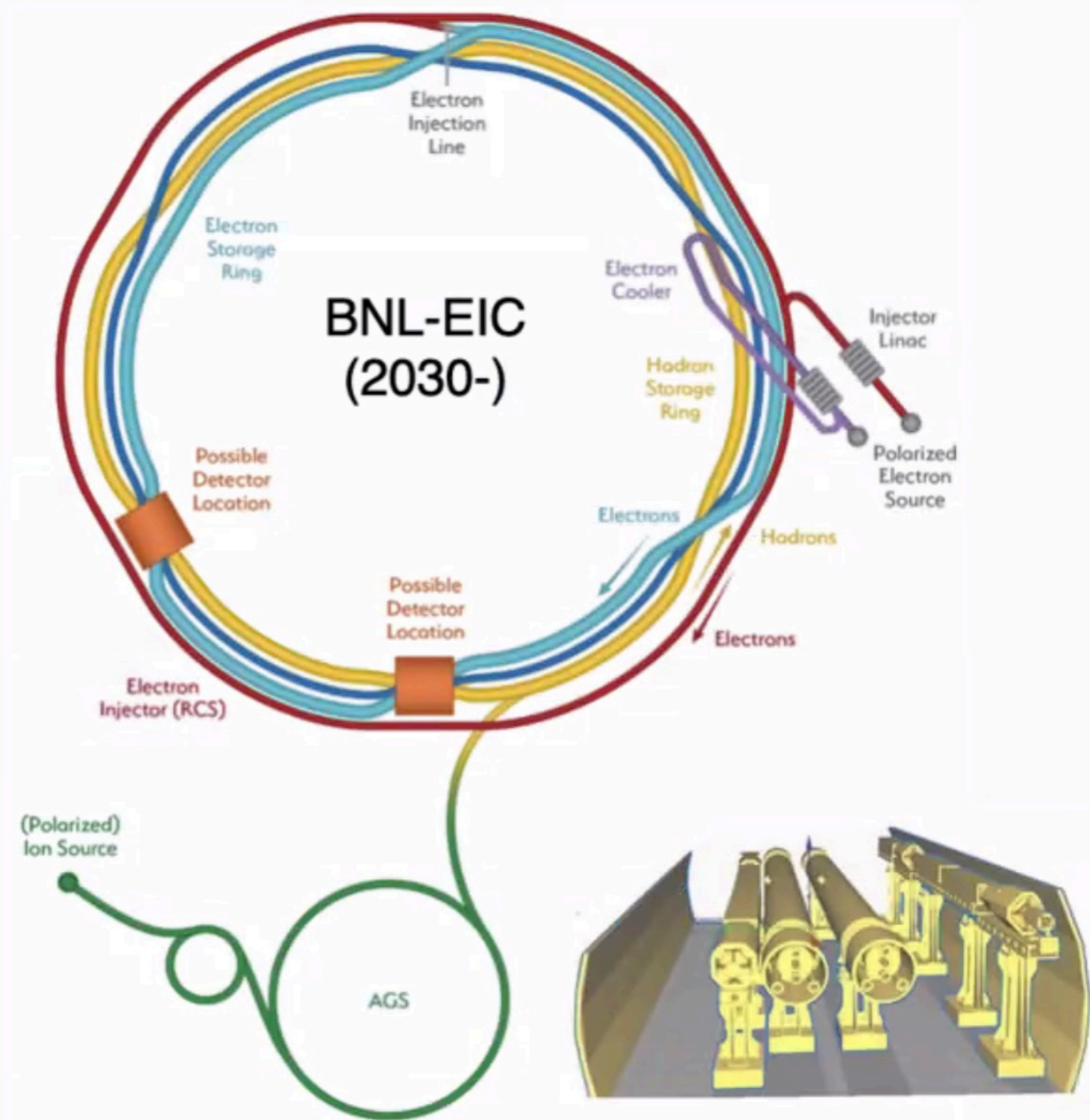


pp, pA, AA up to 500 GeV

ep, eA up to 140 GeV



upgrade



Electron-Ion Collider at BNL



One of hadron storage rings is re-used.

ep, eA up to 140 GeV

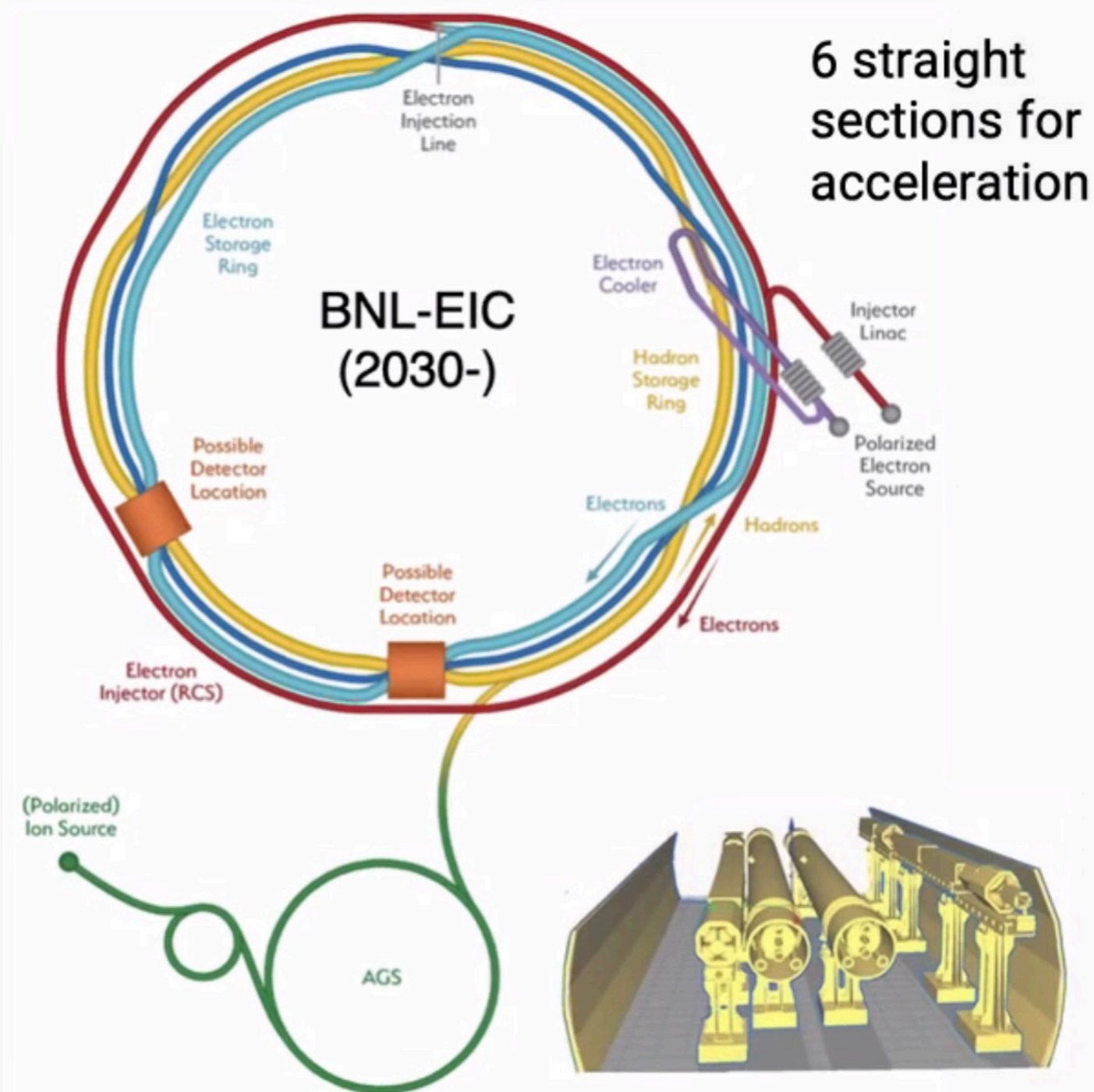
RHIC infrastructure (existing tunnel) is re-used as much as possible.

Additions to RHIC:

- Polarized electron source
- LINAC
- Rapid-cycling synchrotron (RCS) in the RHIC tunnel.
- A new electron storage ring in the RHIC tunnel.

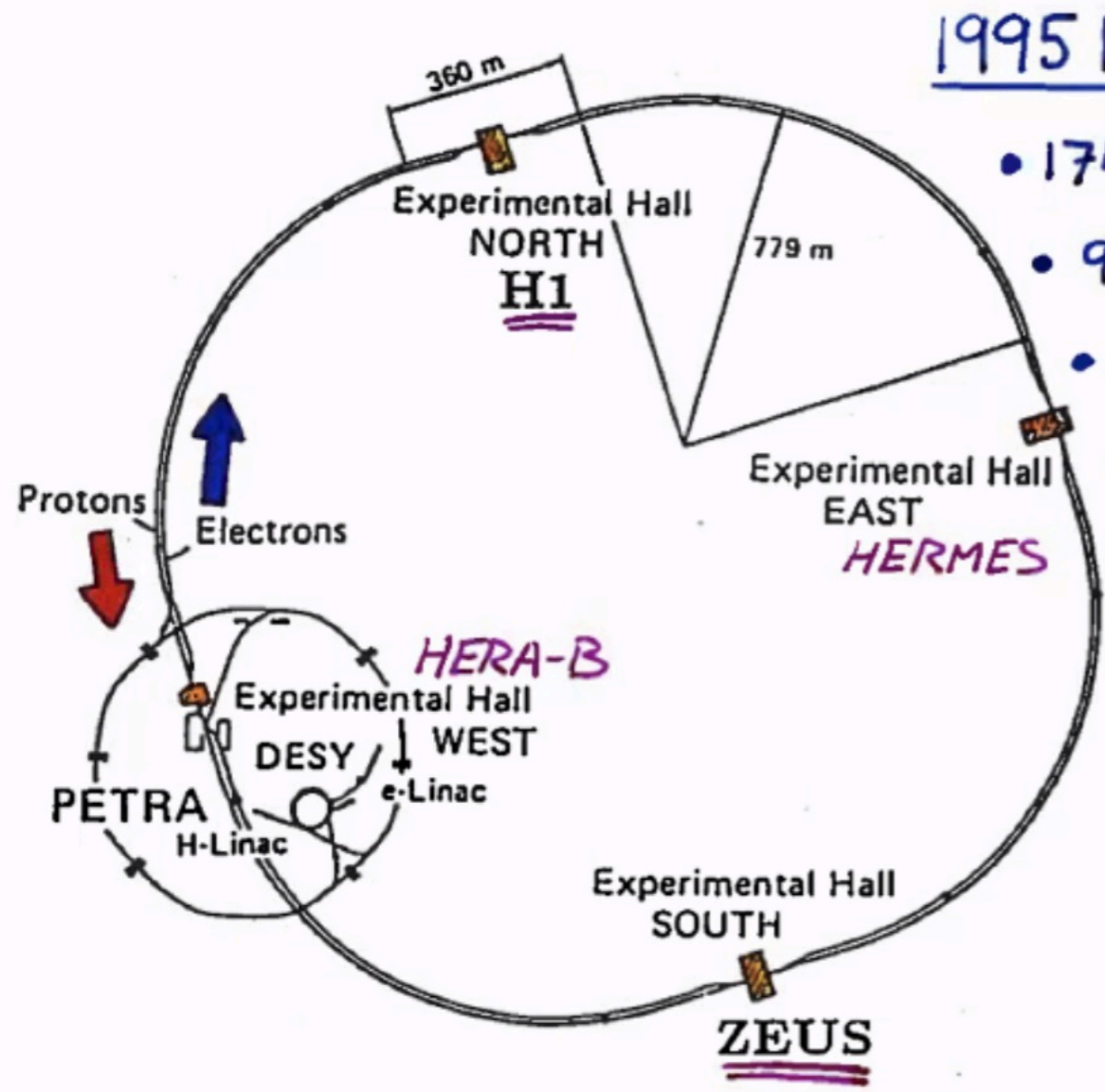
Cost: \$1.6-2.6B (DOE-NP).

- U.S. accounting, including detectors





HERA

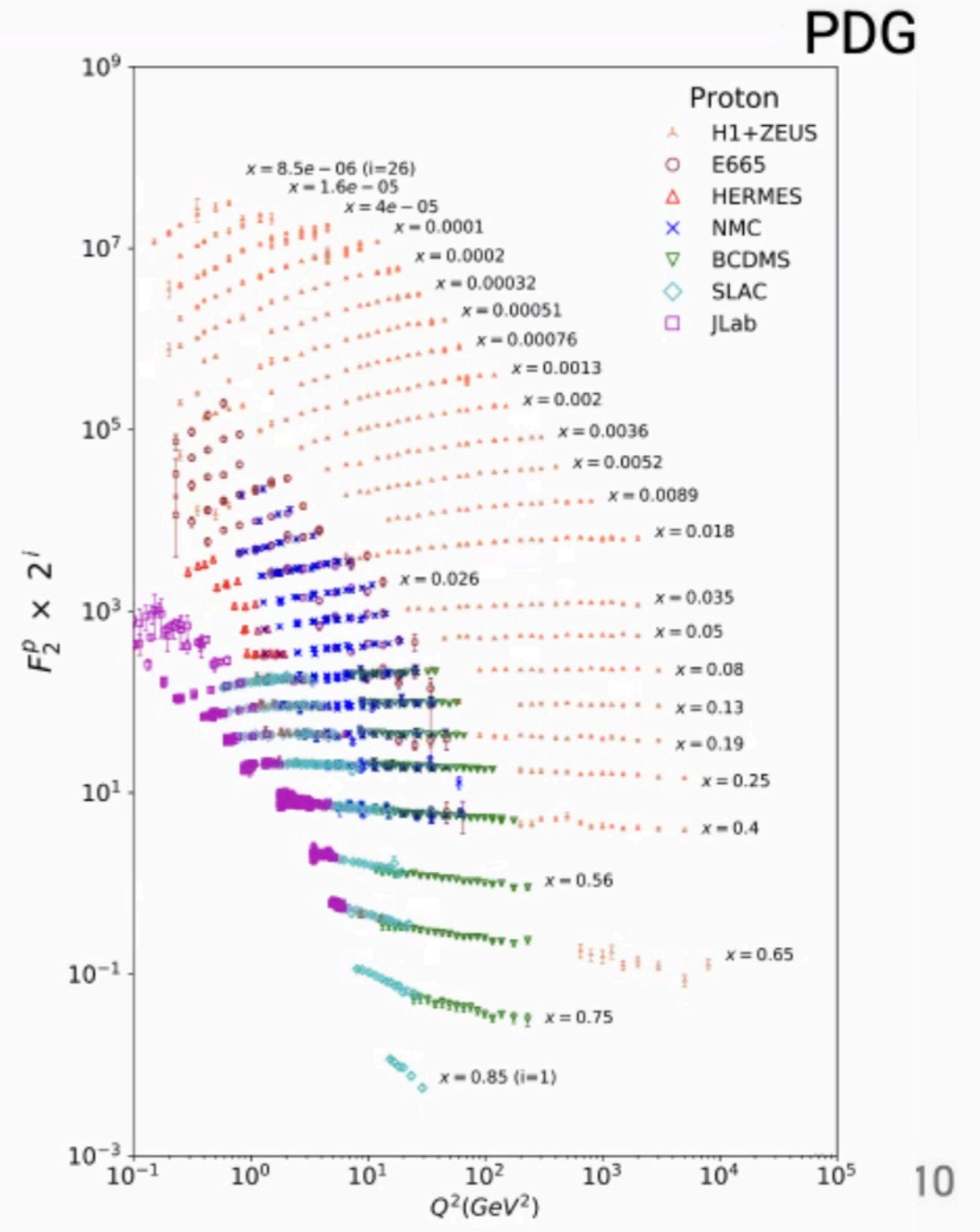


1995 Parameters:

- 174 bunches
- 96ns spacing
- $I_e = 30\text{mA}$
- $I_p = 65\text{mA}$

27.5 GeV e^\pm on 920 GeV p $\rightarrow \sqrt{s} = 318$ GeV

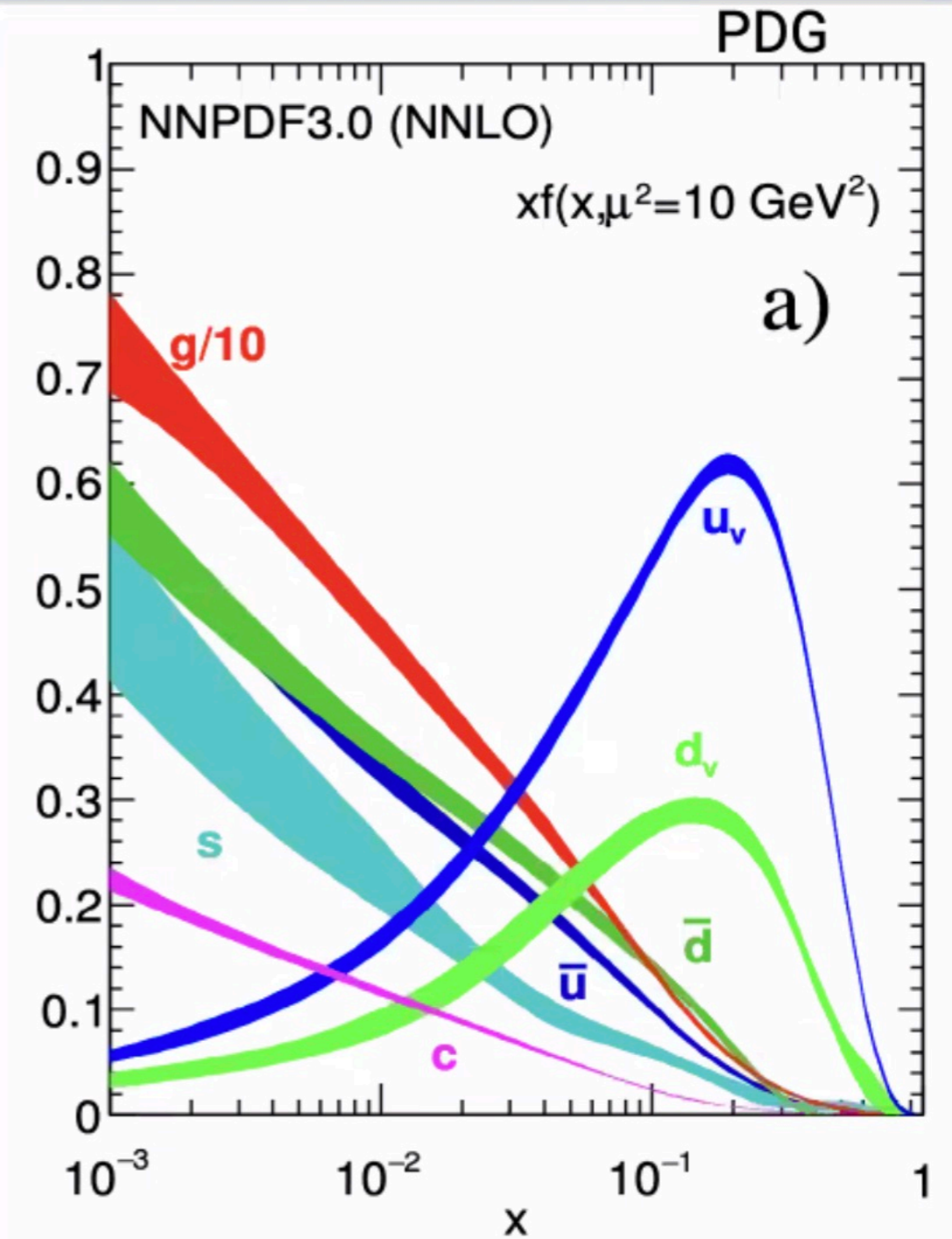
- HERA probed a completely new DIS regime from earlier fixed target experiments



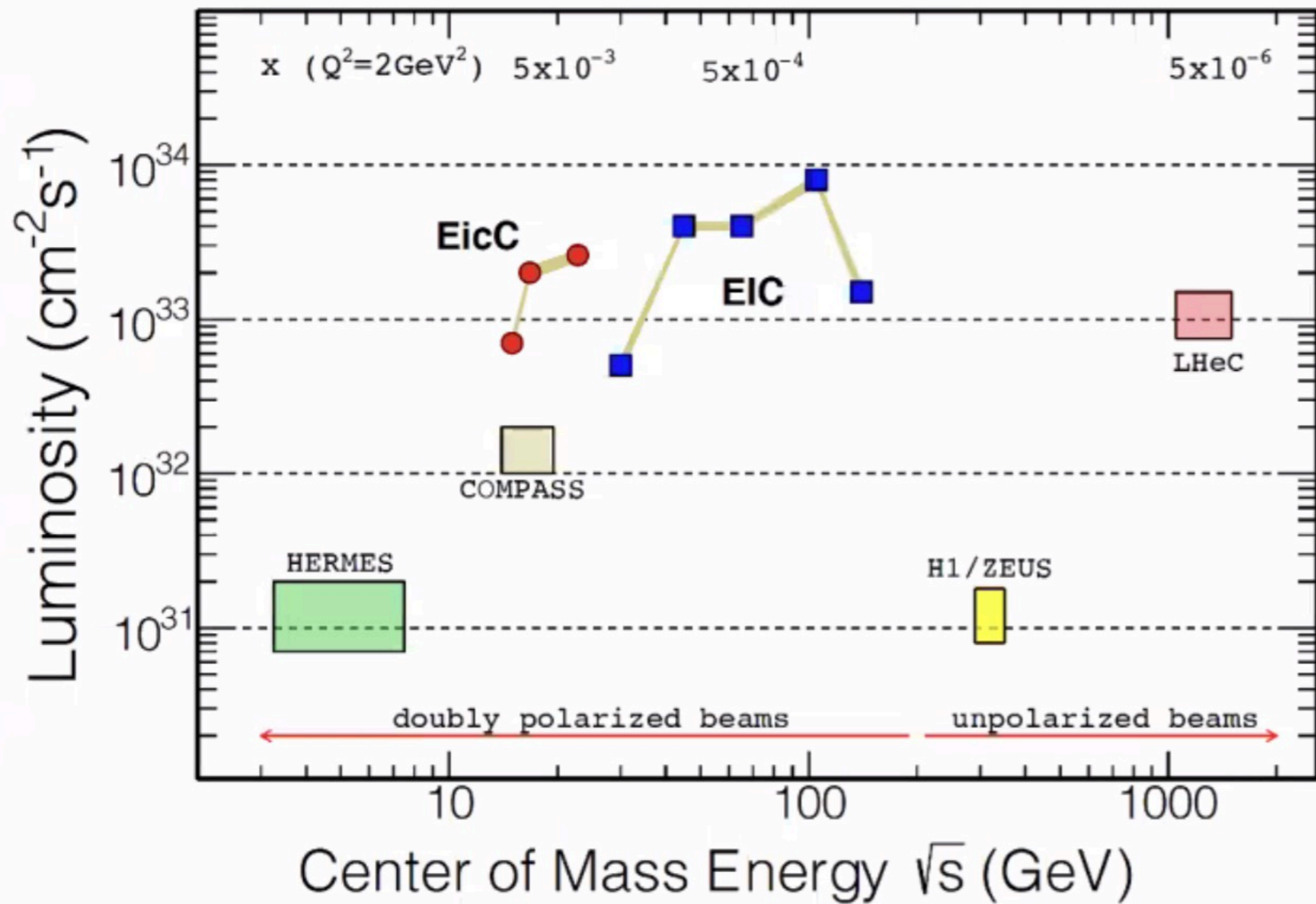
Parton Densities



- HERA paved the way for precision LHC physics through precise structure function measurements, from which the parton densities are extracted through global fits with QCD
- HERA saw the strong rise in the gluon density at low x
 - When do saturation effects come into play?



Lumi vs. \sqrt{s} at lepton-hadron colliders



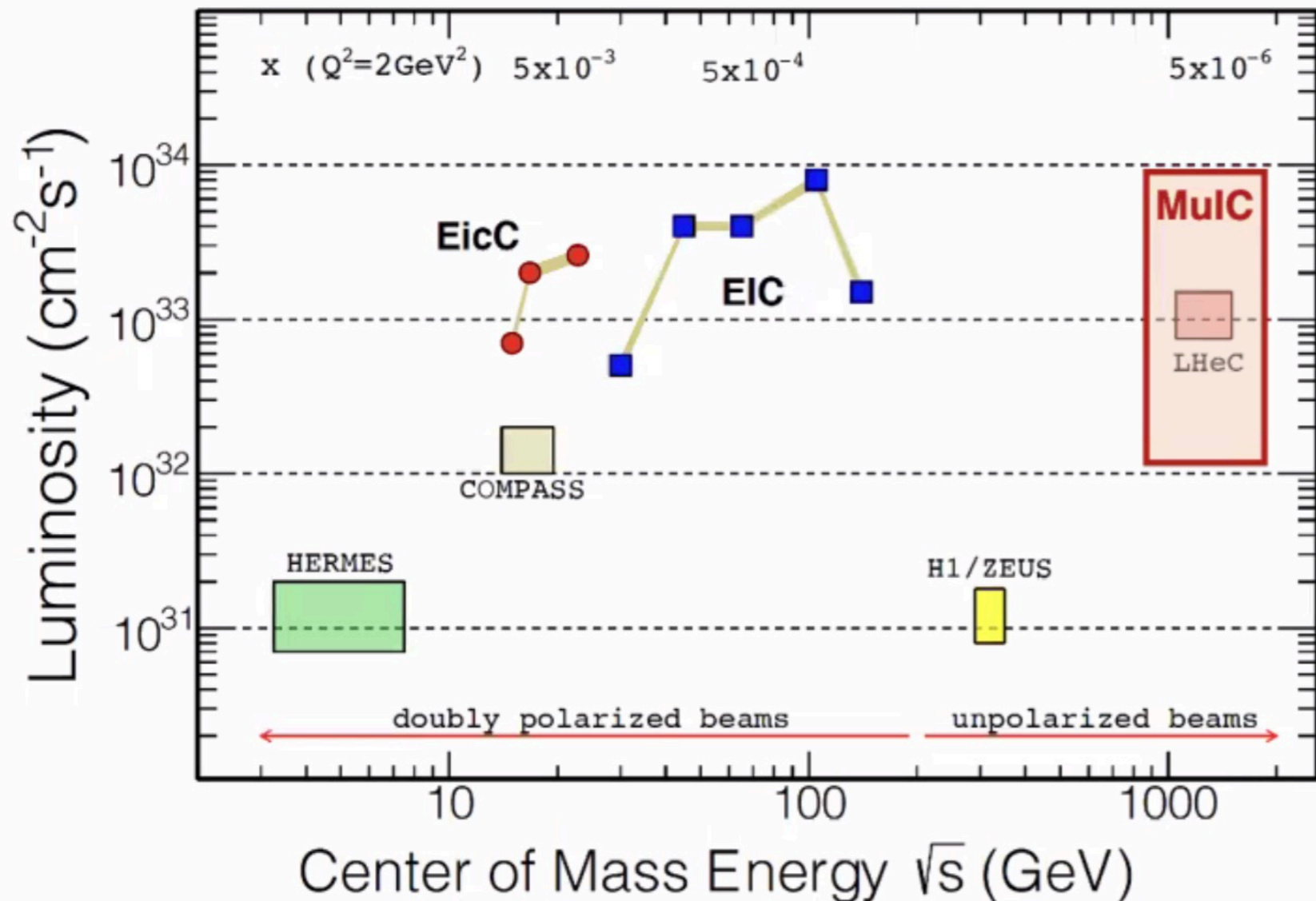
HERA at DESY – high energy but low luminosity, unpolarized or singly polarized (*)

EIC at BNL – lowish energy but high luminosity, doubly polarized, ions

What's after EIC?

- LHeC (arXiv:2007.14491)?

(*) HERA-II did achieve longitudinally polarized electron beams



HERA at DESY – high energy but low luminosity, unpolarized

EIC at BNL – lowish energy but high luminosity, doubly polarized, ions

What's after EIC?

- LHeC ([arXiv:2007.14491](https://arxiv.org/abs/2007.14491))?
- **Muon-Ion Collider at BNL!**
(esp. with polarized muons)

A Muon-Ion Collider: Who Ordered That?



Probe a **new energy scale** and nucleon momentum fraction in Deep Inelastic Scattering using a relatively compact machine

- $\sqrt{s} \sim 1 \text{ TeV}$
 - Q^2 up to 10^6 GeV^2
 - x as low as 10^{-6}
- } **An order of magnitude beyond the HERA ep collider**

Build a science case for **a TeV muon storage ring** as a demonstrator toward a multi-TeV $\mu^+\mu^-$ collider

- QCD and hadron/nucleon structure in new regimes
- Higgs, Top, BSM

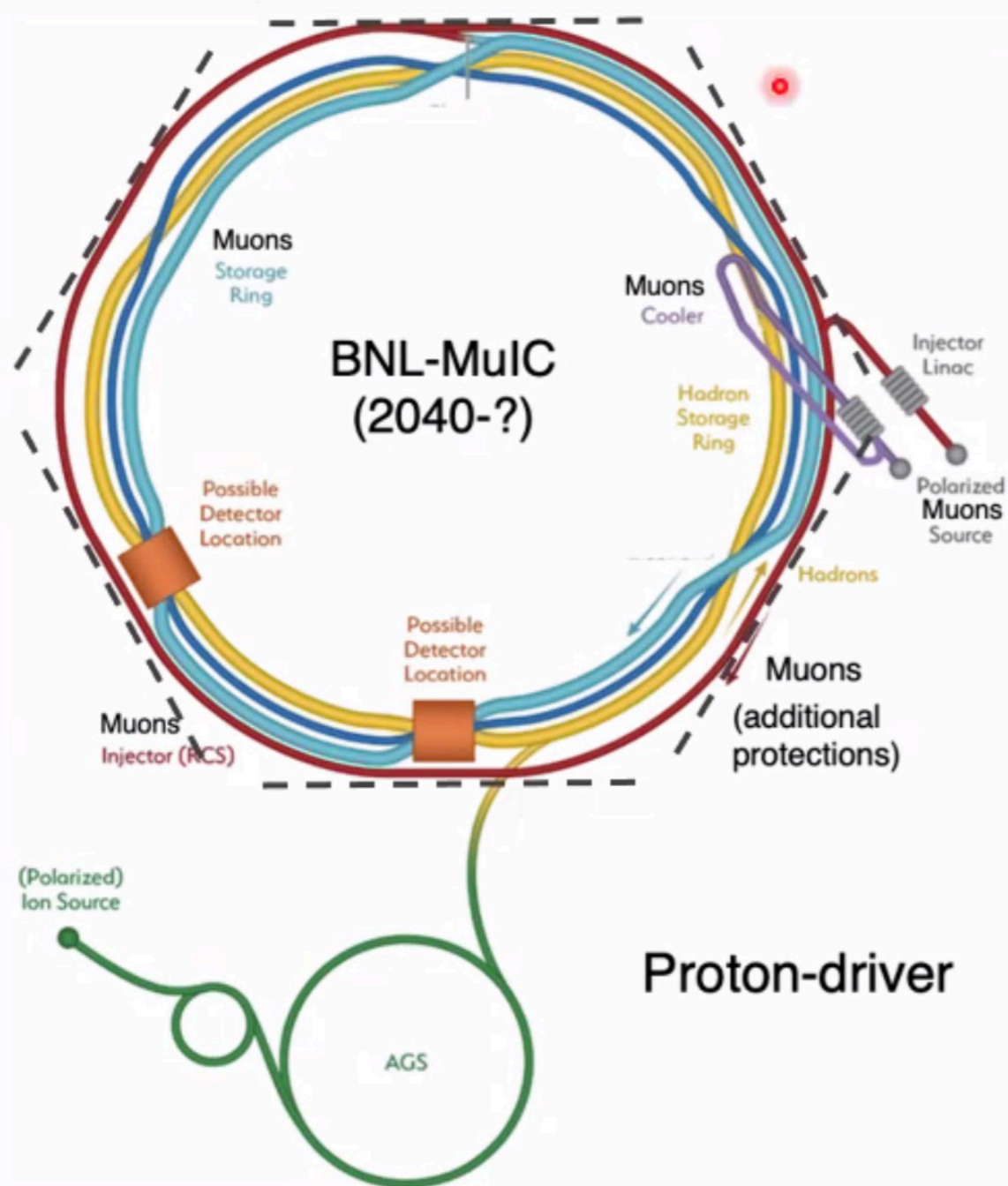
Facilitate the collaboration of the **nuclear and particle physics communities** around an innovative and forward-looking machine

Re-use existing facilities at BNL (MuIC as an upgrade to the EIC)

Muon-Ion Collider at BNL



replace e by μ beam



Bending radius of RHIC tunnel: $r = 290\text{m}$

Achievable muon beam energy: $0.3Br$

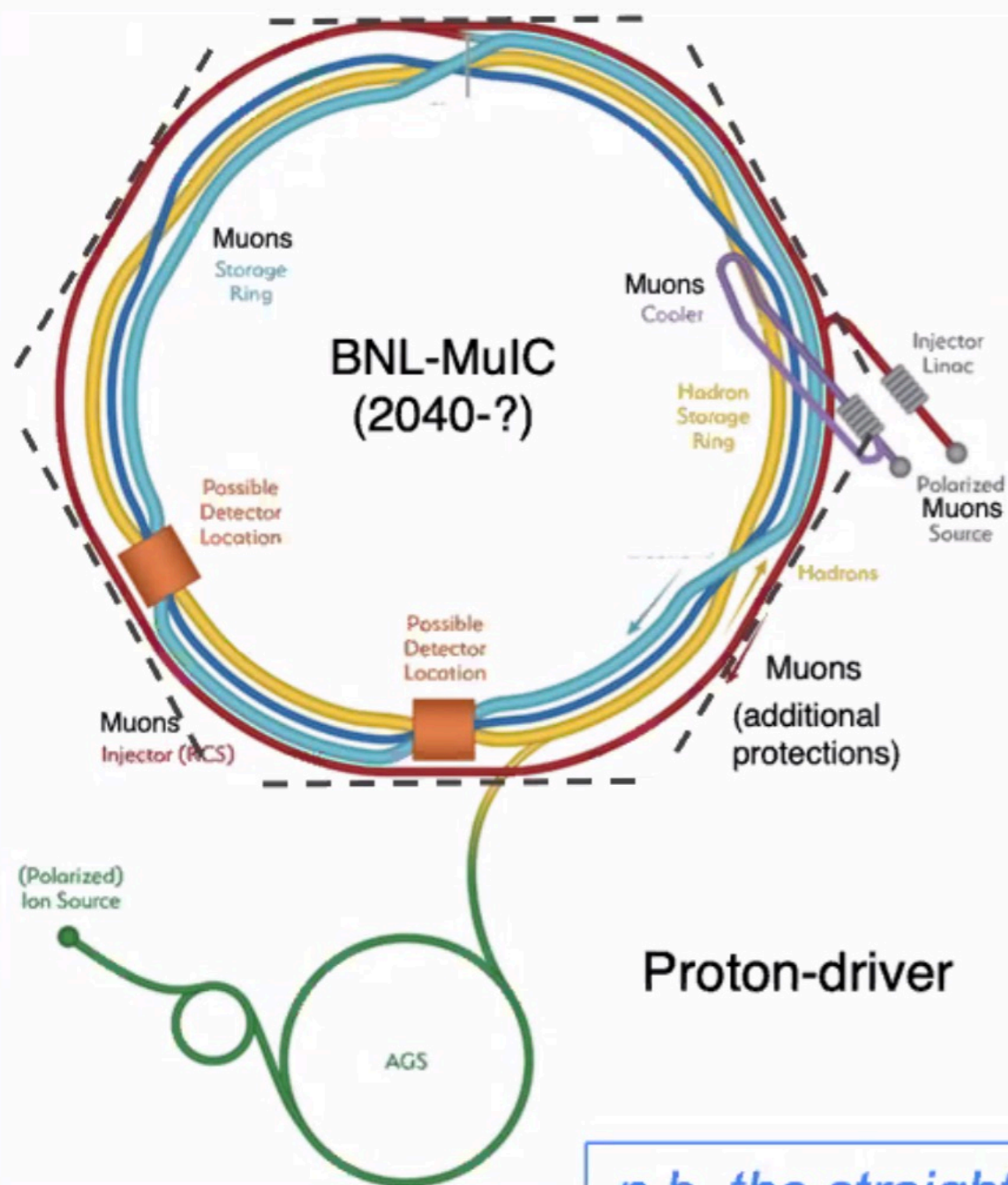
Parameter	1 (aggressive)	2 (realistic)	3 (conservative)
Muon energy (TeV)	1.39	0.96	0.73
Muon bending magnets (T)	16 (FCC)	11 (HL-LHC)	8.4 (LHC)
Muon bending radius (m)	290		
Proton (Au) energy (TeV)	0.275 (0.11/nucleon)		
CoM energy (TeV)	1.24 (0.78)	1.03 (0.65)	0.9 (0.57)

7-8X increase over top EIC energy

Muon-Ion Collider at BNL



replace e by μ beam



Bending radius of RHIC tunnel: $r = 290\text{m}$

Achievable muon beam energy: $0.3Br$

Parameter	1 (aggressive)	2 (realistic)	3 (conservative)
Muon energy (TeV)	1.39	0.96	0.73
Muon bending magnets (T)	16 (FCC)	11 (HL-LHC)	8.4 (LHC)
Muon bending radius (m)		290	
Proton (Au) energy (TeV)		0.275 (0.11/nucleon)	
CoM energy (TeV)	1.24 (0.78)	1.03 (0.65)	0.9 (0.57)

7-8X increase over top EIC energy

n.b. the straight sections would provide collimated beams of neutrinos as well



Luminosity estimate:

$$f_c^\mu = f_{\text{rep}} * N_c$$

$$\mathcal{L}_{\mu p} = \frac{N^\mu N^p}{4\pi \max[\sigma_x^\mu, \sigma_x^p] \max[\sigma_y^\mu, \sigma_y^p]} \min[f_c^\mu, f_c^p] H_{hg}$$

arXiv:1905.05564

Parameter	Muon	Proton
Energy (TeV)	0.96	0.275
CoM energy (TeV)	1.03	
Bunch intensity (10^{11})	20	3
Norm. emittance, $\epsilon_{x,y}$ (μm)	25	0.2
$\beta_{x,y}^*$ @IP (cm)	1	5
Trans. RMS beam size, $\sigma_{x,y}$ (μm)	5.2	5.8
Muon repetition rate, f_{rep} (Hz)	15	
Cycles/Collisions per muon bunch, N_c	3279 (~300B)	
$\mathcal{L}_{\mu p}$ ($10^{33}\text{cm}^{-2}\text{s}^{-1}$)		7

Muon beam (MAP):

arXiv:1901.06150

Table 1: Main parameters of the proton driver muon facilities

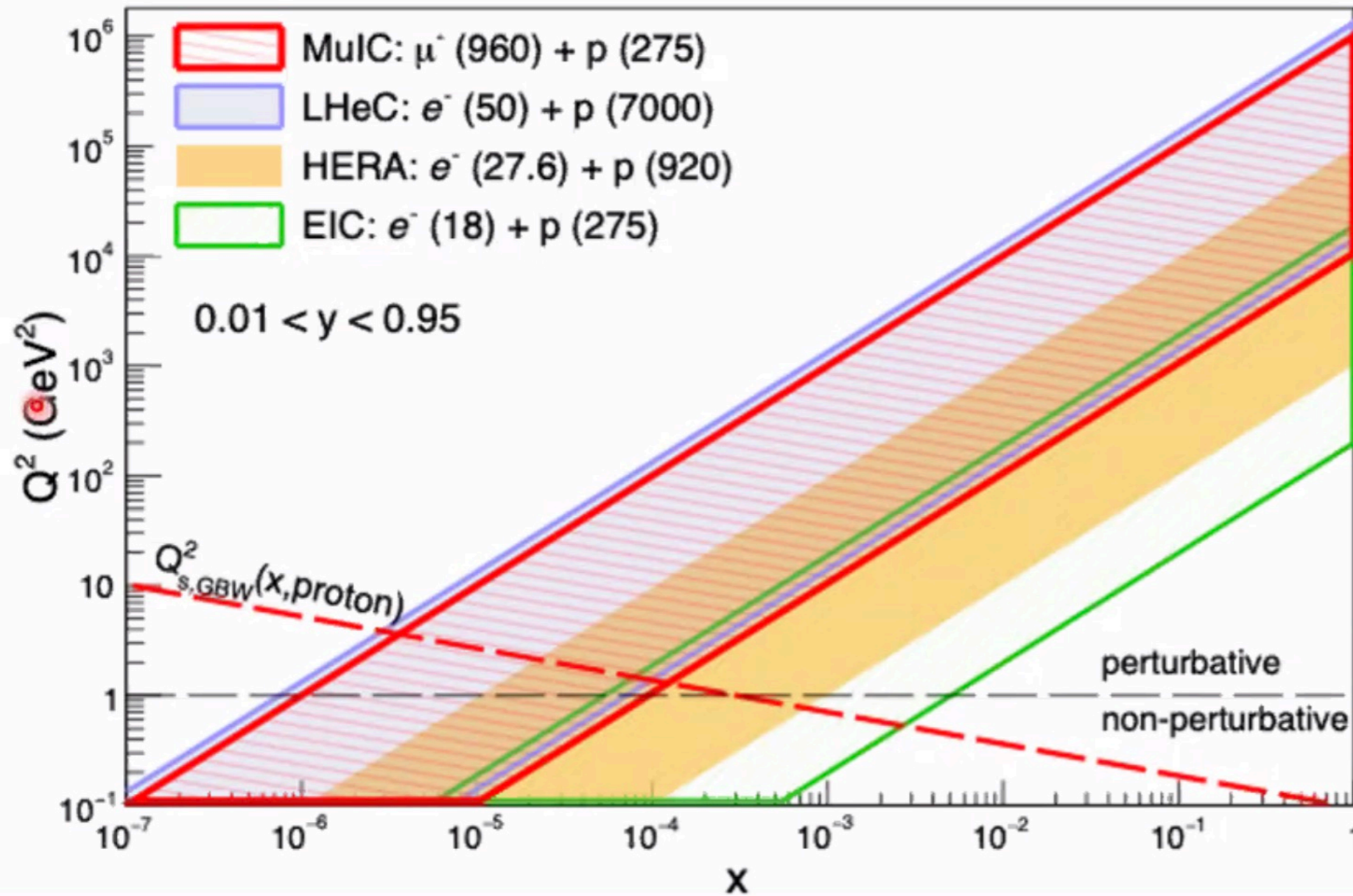
Parameter	Units	Higgs	Multi-TeV
CoM Energy	TeV	0.126	1.5, 3.0, 6.0
Avg. Luminosity	$10^{34}\text{cm}^{-2}\text{s}^{-1}$	0.008	1.25, 4.4, 12
Beam Energy Spread	%	0.004	0.1, 0.1, 0.1
Higgs Production/ 10^7 sec		13'500	37'500, 200'000, 820'000
Circumference	km	0.3	2.5, 4.5, 6
No. of IP's		1	2, 2, 2
Repetition Rate	Hz	15	15, 12, 6
$\beta_{x,y}^*$	cm	1.7	1, 0.5, 0.25
No. muons/bunch	10^{12}	4	2, 2, 2
Norm. Trans. Emittance, ϵ_{TN}	$\mu\text{m-rad}$	200	25, 25, 25
Norm. Long. Emittance, ϵ_{LN}	$\mu\text{m-rad}$	1.5	70, 70, 70
Bunch Length, σ_S	cm	6.3	1, 0.5, 0.2
Proton Driver Power	MW	4	4, 4, 1.6
Wall Plug Power	MW	200	216, 230, 270

Polarized proton beam from eRHIC/EIC

arXiv:1409.1633

And the more experimental interaction points, the better before the muons decay...

Q^2 - x Reach Comparison: $e(\mu)$ - p Scattering



Well beyond the coverage of the EIC and HERA

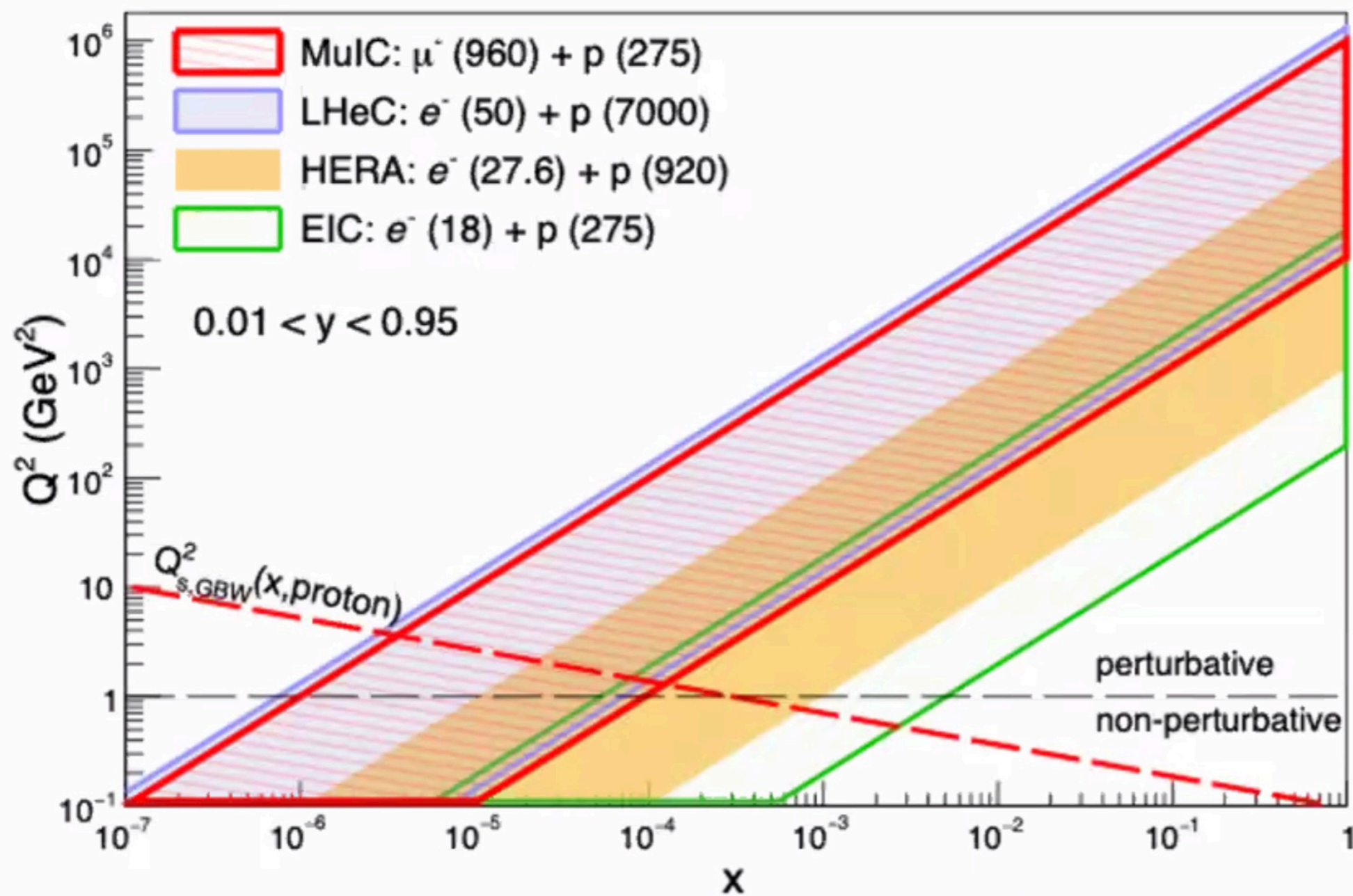
Similar coverage to the proposed Large Hadron Electron Collider **LHeC** [1]

Potential to see gluon saturation [2] in the proton

[1] LHeC: [arXiv:2007.14491](https://arxiv.org/abs/2007.14491)

[2] GBW model: [Phys. Rev. D 59, 014017 \(1998\)](https://doi.org/10.1103/PhysRevD.59.014017)

Q²-x Reach Comparison: e(μ)-p Scattering



Well beyond the coverage of the EIC and HERA

Similar coverage to the proposed Large Hadron Electron Collider **LHeC** [1]

Potential to see gluon saturation [2] in the proton

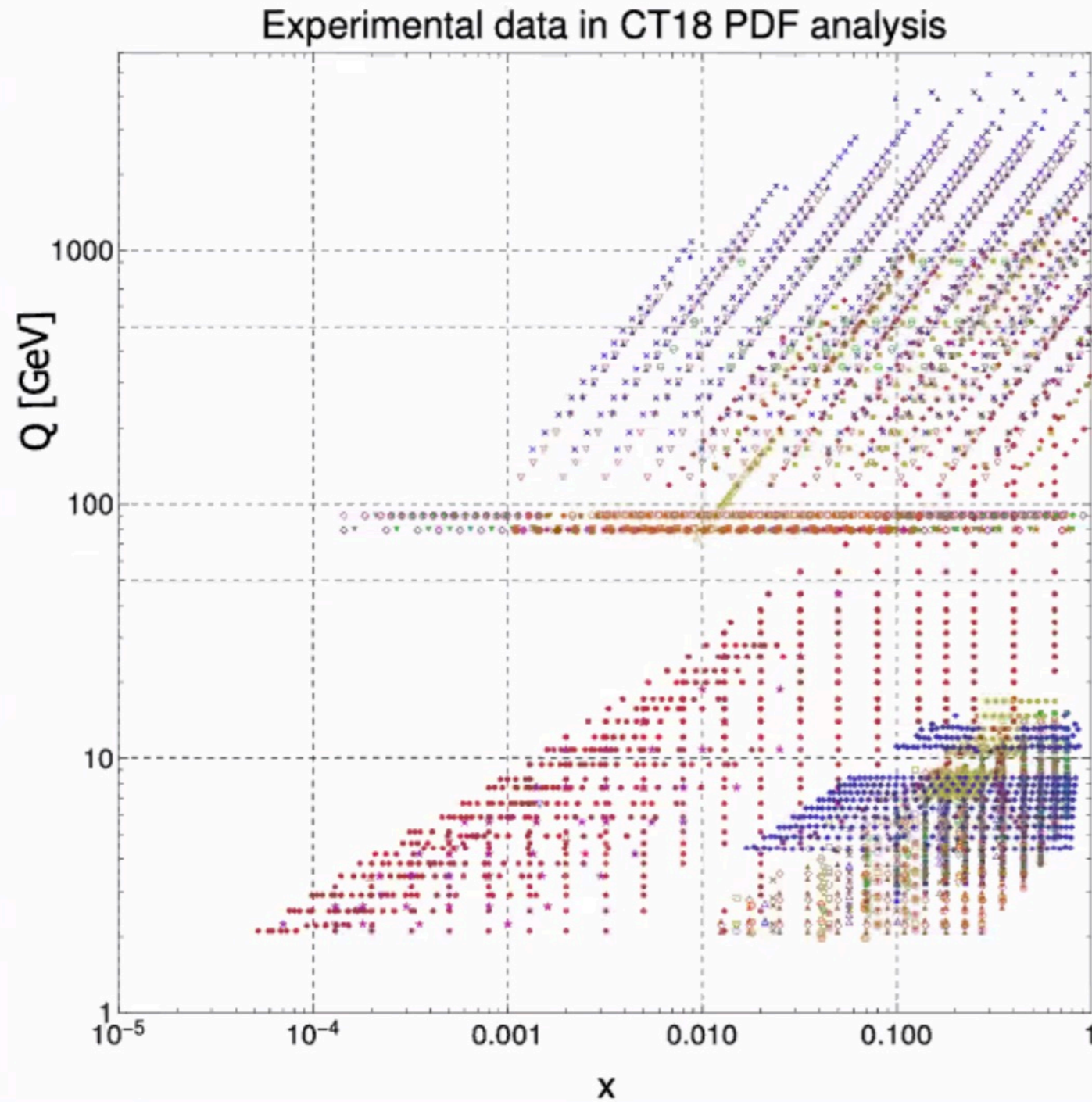
[1] LHeC: [arXiv:2007.14491](https://arxiv.org/abs/2007.14491)

[2] GBW model: [Phys. Rev. D 59, 014017 \(1998\)](https://doi.org/10.1103/PhysRevD.59.014017)

MuIC: μ(960)+p(275), $y_{cm} = -0.63$ vs. LHeC: e(50)+p(7000), $y_{cm} = 2.47$

Similar \sqrt{s} but very different final-state kinematics

Science potential at the MuIC: PDF Measurements

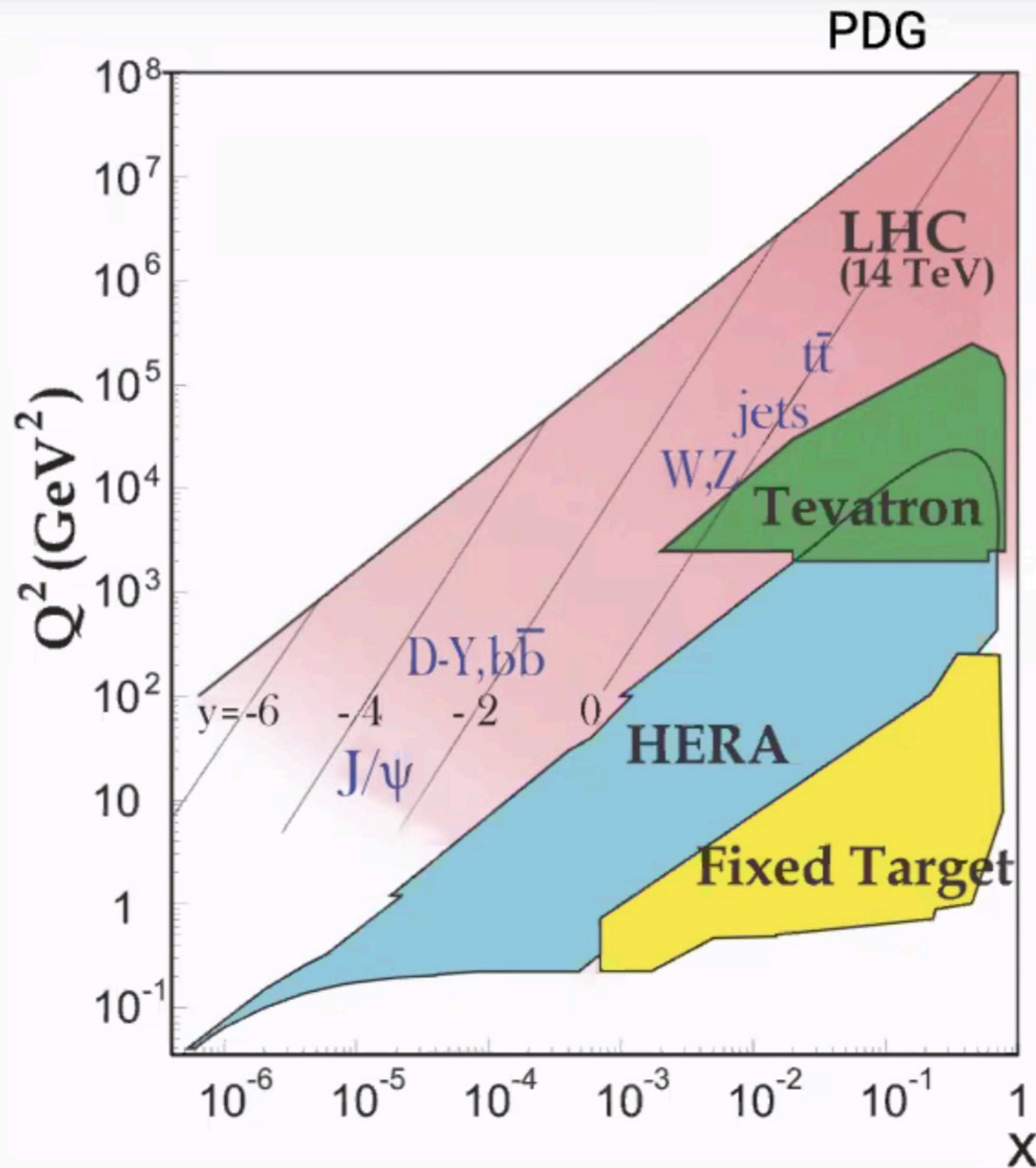


CTEQ, [arXiv:1912.10053](https://arxiv.org/abs/1912.10053)

- | | |
|------------------|------------------------|
| ● HERA1+IF15 | ◇ ZyCDF2'10 |
| ■ BCDMSp'89 | △ HERAb'06 |
| ◆ BCDMSd'90 | ▽ HERA-FL'11 |
| ▲ NMCrat97 | × CMS7EASY'12 |
| ▼ CDHSW-F2'91 | ⊖ ATL7WZ'12 |
| ○ CDHSW-F3'91 | • D02EASY2'15 |
| □ CCFR-F2'01 | ● CMS7Masy2'14 |
| ◇ CCFR-F3'97 | ■ CDF2JETS'09 |
| △ NuTeV-NU'06 | ◆ D02JETS'08 |
| ▽ NuTeV-NUB'06 | ▲ ATLAS7JETS'15 |
| × CCFR SI NU'01 | ▼ LHCb7ZWRAP'15 |
| ⊖ CCFR SI NUB'01 | ○ LHCb8ZEE'15 |
| • HERAc'13 | □ CMS8Wasy'16 |
| ● E605'91 | ◇ LHCb8WZ'16 |
| ■ E866RAT'01 | △ ATLASZpT'16 |
| ◆ E866PP'03 | ▽ CMS7JETS'14 |
| ▲ CDF1Wasy'96 | × CMS8JETS'17 |
| ▼ CDF2Wasy'05 | ⊖ CMS8TTB-pTtyt'17 |
| ○ D02Masy'08 | • ATLAS8TTB-pTt-MTT'15 |
| □ ZyD02'08 | ● ATL7ZW'16 |

← Data used for global CTEQ fits

The MuIC would definitely probe new territory



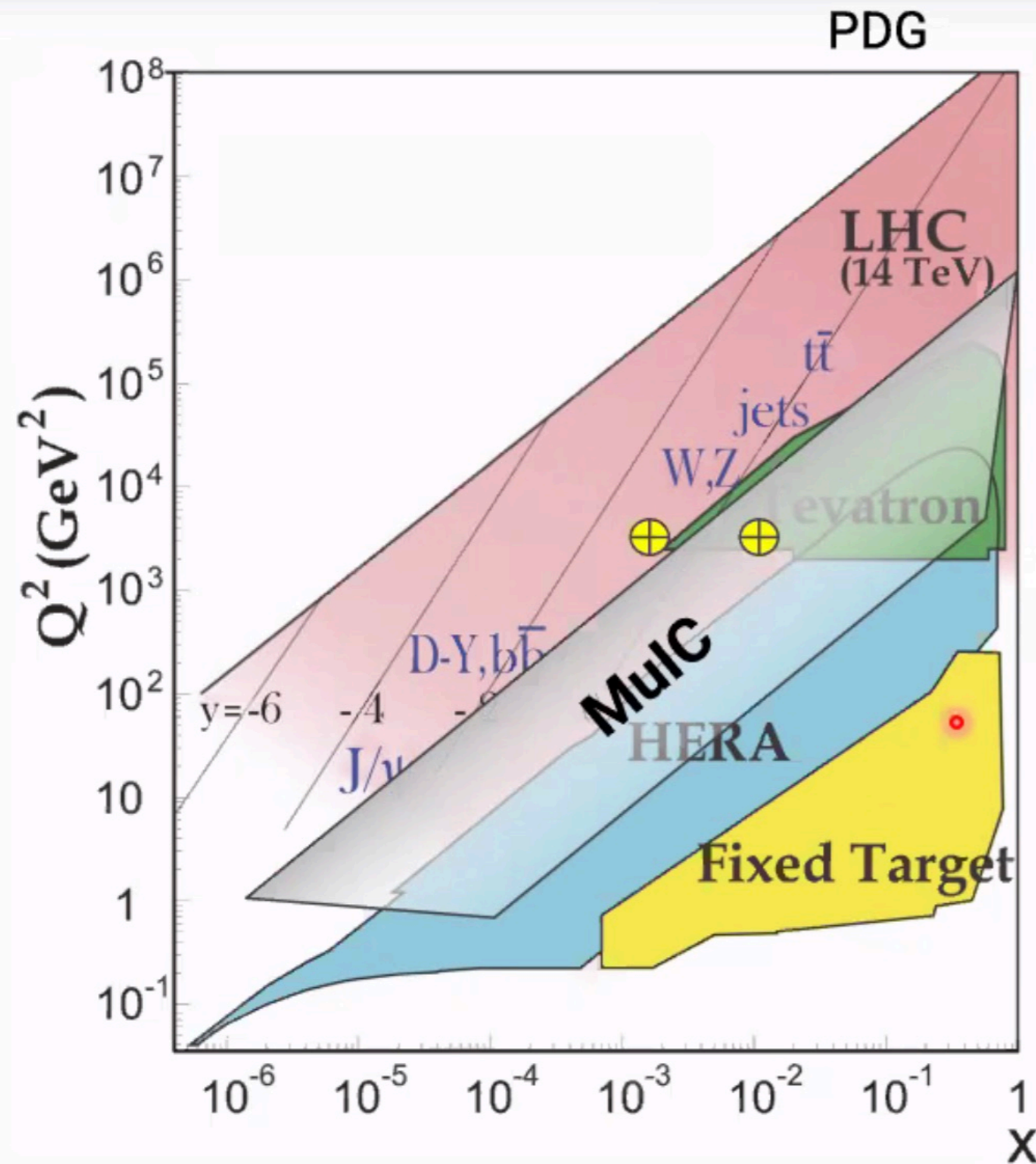
LHC data also can be used to extract parton densities from Drell-Yan, W, jet, and top production measurements

- But it's a bit circular when also trying to measure those cross sections...
- Also convoluted with QCD effects and quark flavor

DIS measurements can more cleanly decouple quark flavor and QCD effects

The MuIC also can directly probe parton densities at the scale for Higgs production at the (HL)LHC, and for a future 100 TeV FCChh should one be built

- Less reliant on fit extrapolation → smaller uncertainties on cross sections ($< \sim 1\%$)
- Useful input for an FCChh program
 - As HERA was for the LHC



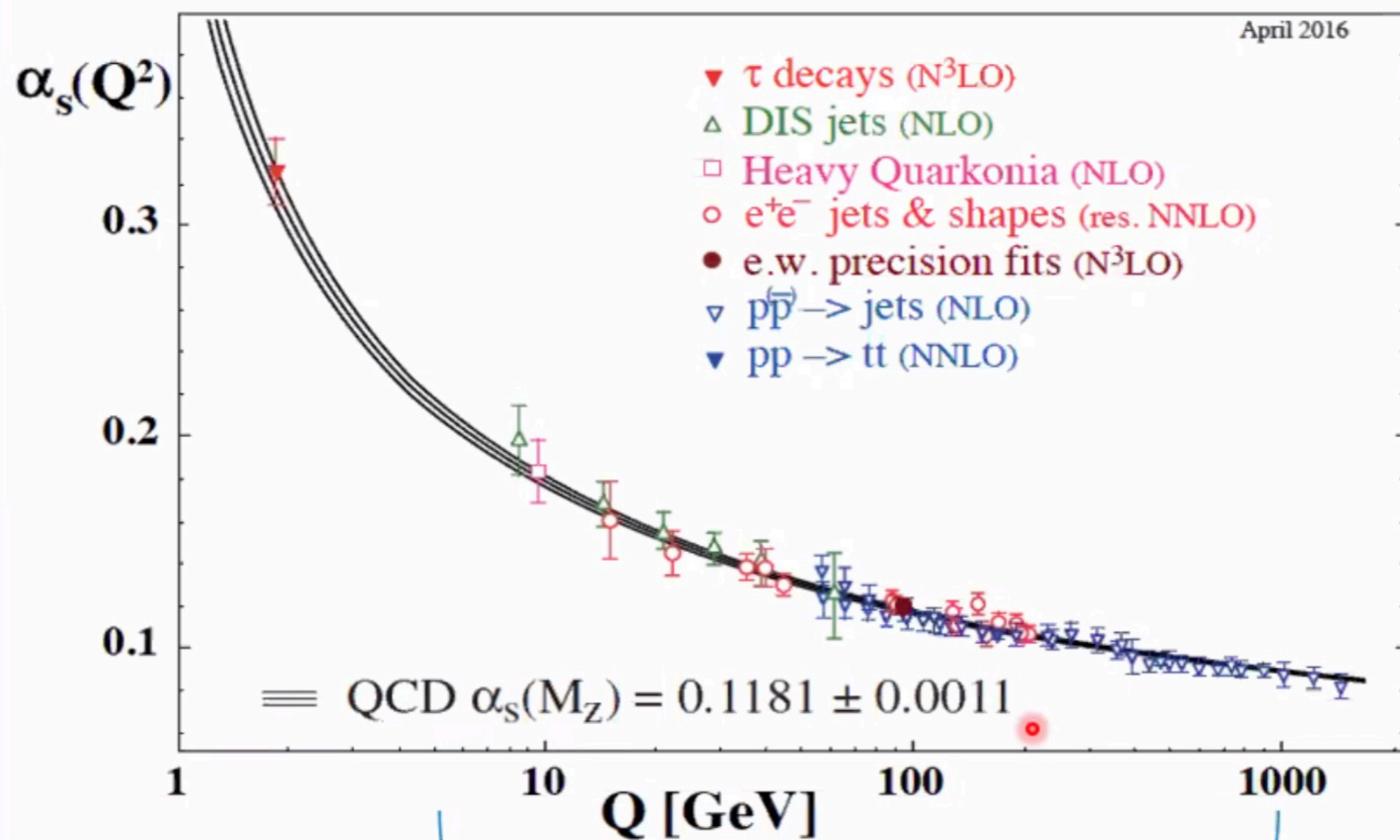
LHC data also can be used to extract parton densities from Drell-Yan, W, jet, and top production measurements

- But it's a bit circular when also trying to measure those cross sections...
- Also convoluted with QCD effects and quark flavor

DIS measurements can more cleanly decouple quark flavor and QCD effects

The MuIC also can directly probe parton densities at the scale for Higgs production at the (HL)LHC, and for a future 100 TeV FCChh should one be built

- Less reliant on fit extrapolation → smaller uncertainties on cross sections ($< \sim 1\%$)
- Useful input for an FCChh program
 - As HERA was for the LHC

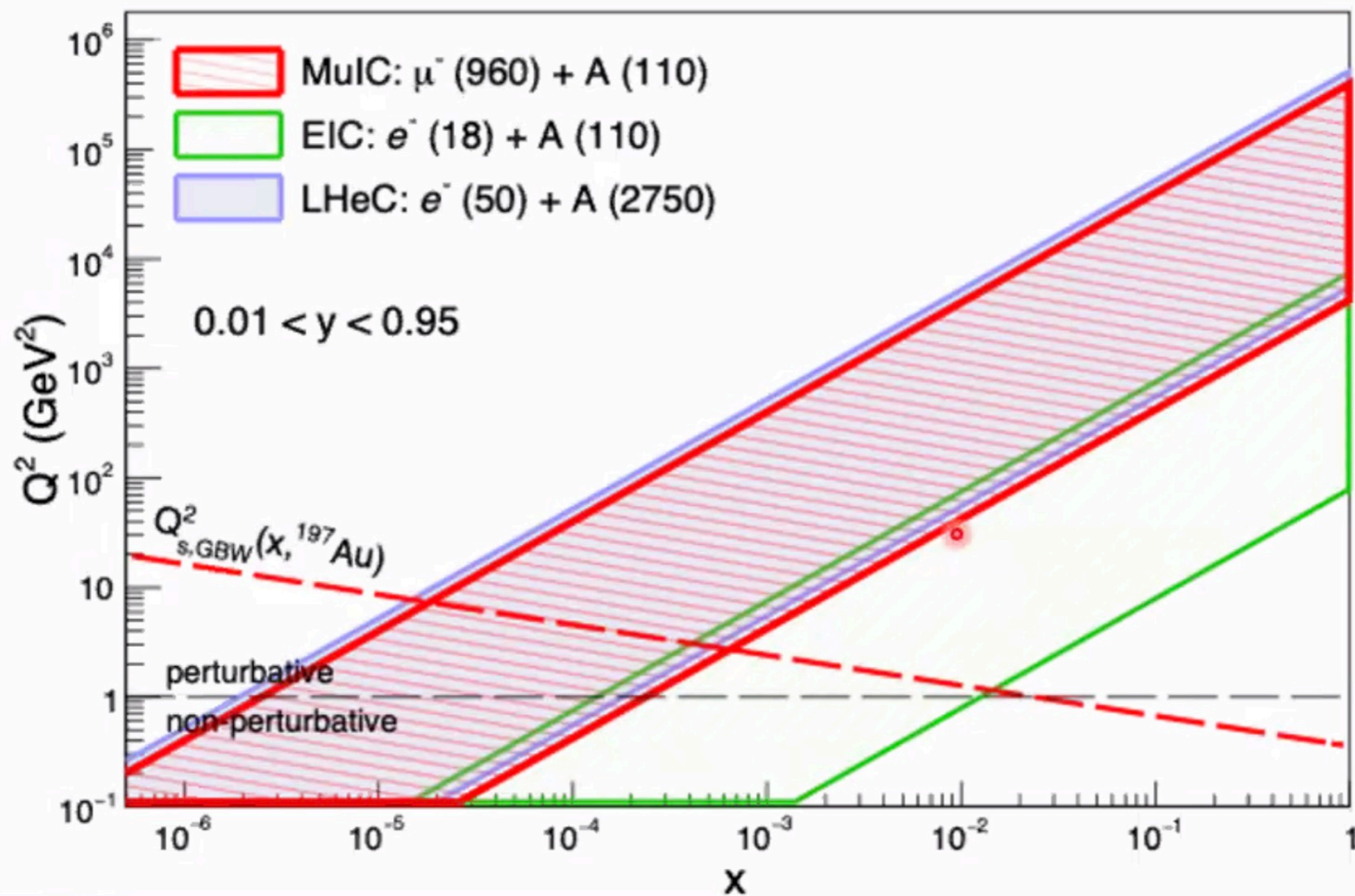


- Measurements can span an even broader range to measure $\alpha_s(Q^2)$ in a single experiment
 - Both from QCD evolution fits to structure function data, and from DIS multijet rate measurements
 - Removes some inter-experiment systematics

Q²-x Reach Comparison: e(μ)-A Scattering



Can explore well the predicted saturation regime [1] in ions



Saturation scale:

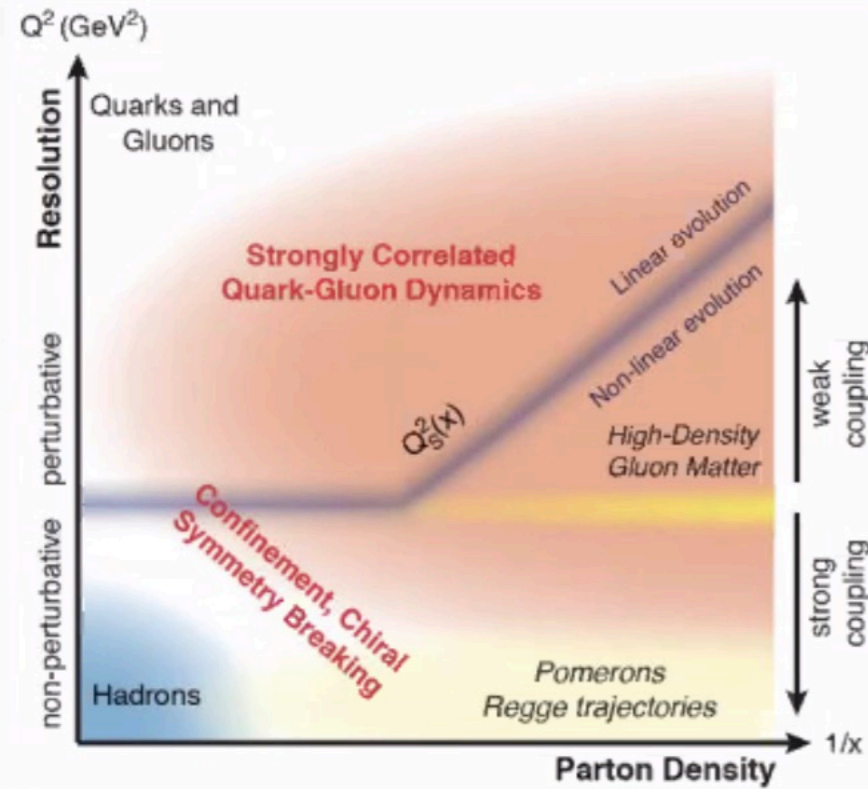
$$Q_s^2(A) = A^{1/3} Q_s^2(p)$$

Also the MuIC can scan a wide range of ion species

[1] GBW model: [Phys. Rev. D 59, 014017 \(1998\)](#)

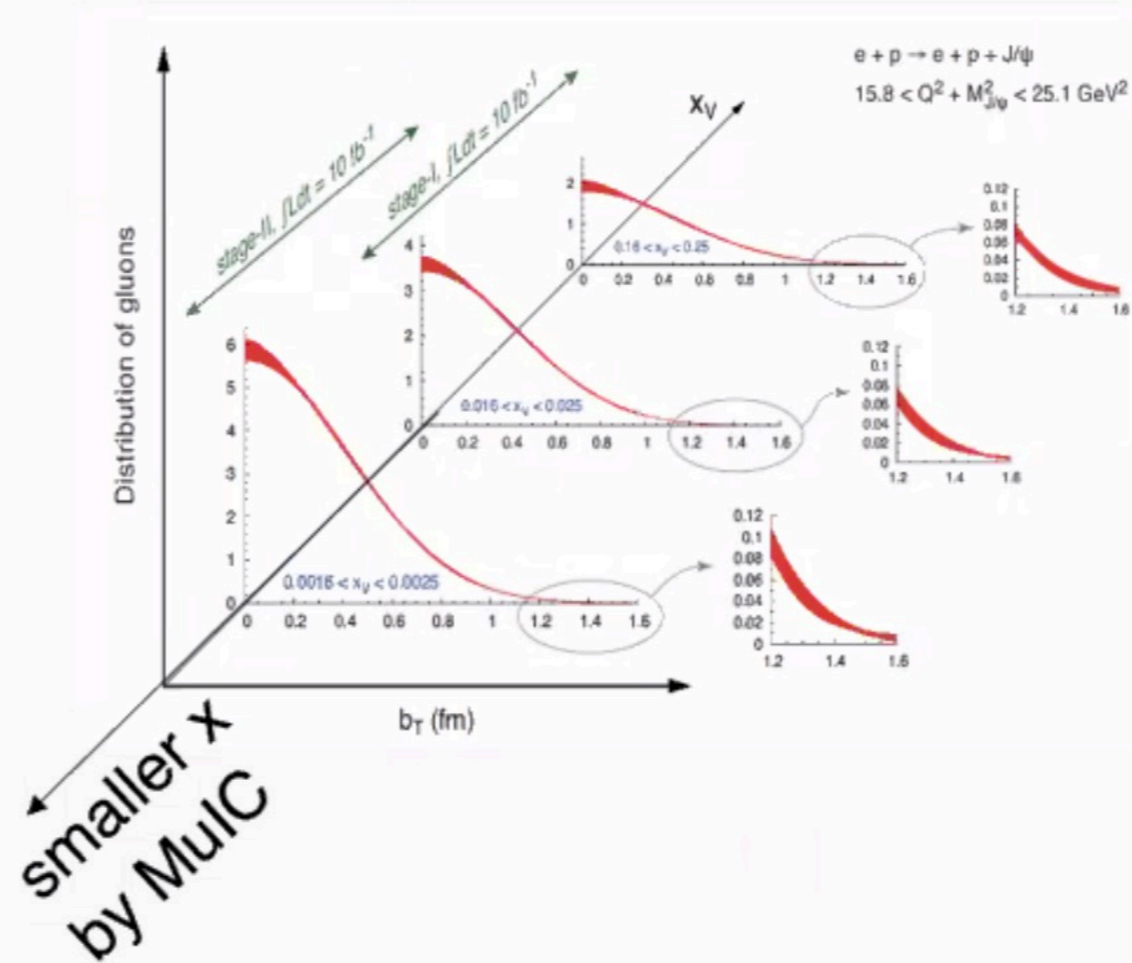


Gluon saturation



What's the property of high-density gluon matter

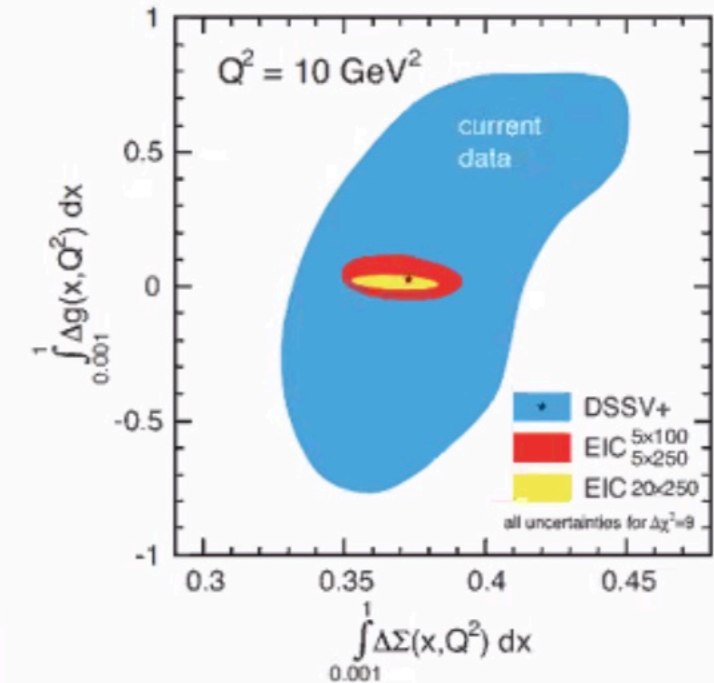
3D Nucleon structure



Nucleon spin puzzle

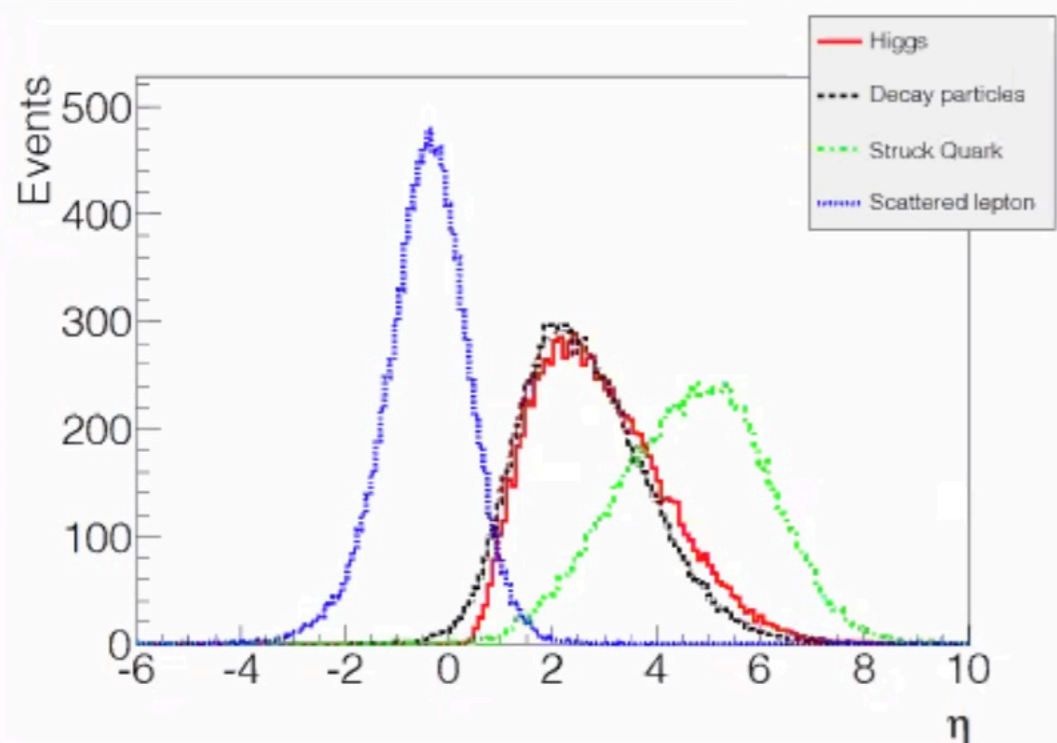
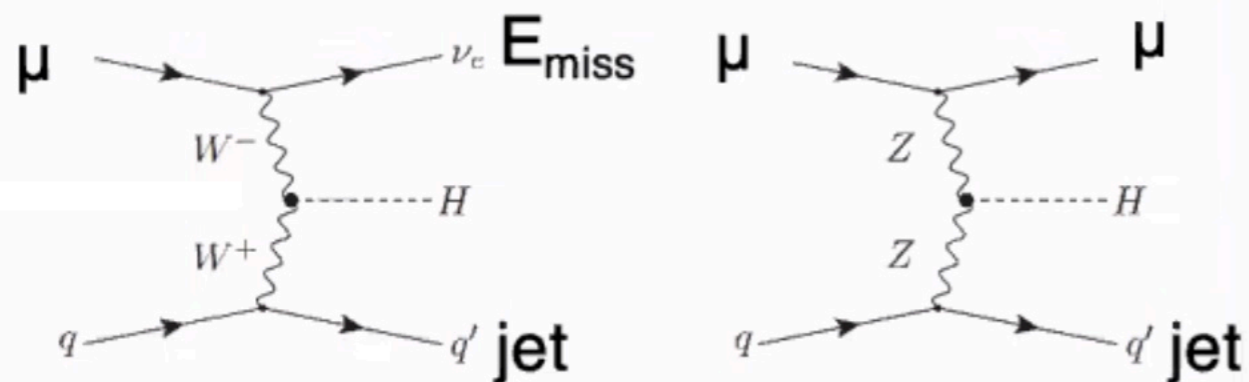
"Helicity sum rule"

$$\frac{1}{2}\hbar = \underbrace{\frac{1}{2}\Delta\Sigma}_{\text{quark contribution}} + \underbrace{\Delta G}_{\text{gluon contribution}} + \underbrace{\sum_q L_q^z + L_g^z}_{\text{orbital angular momentum}}$$

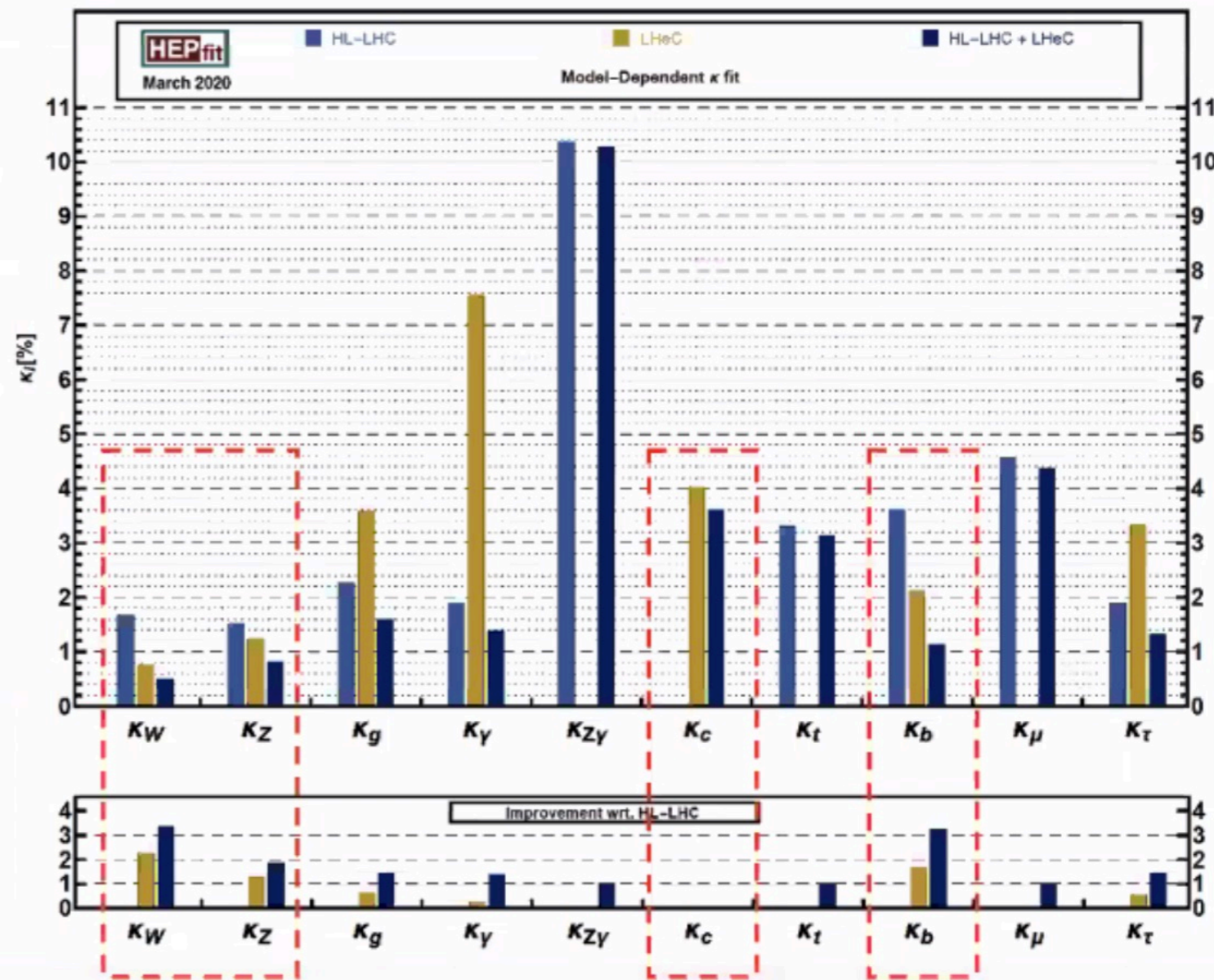


MuIC to reach $x \sim 10^{-5}$

Higgs at the MuIC

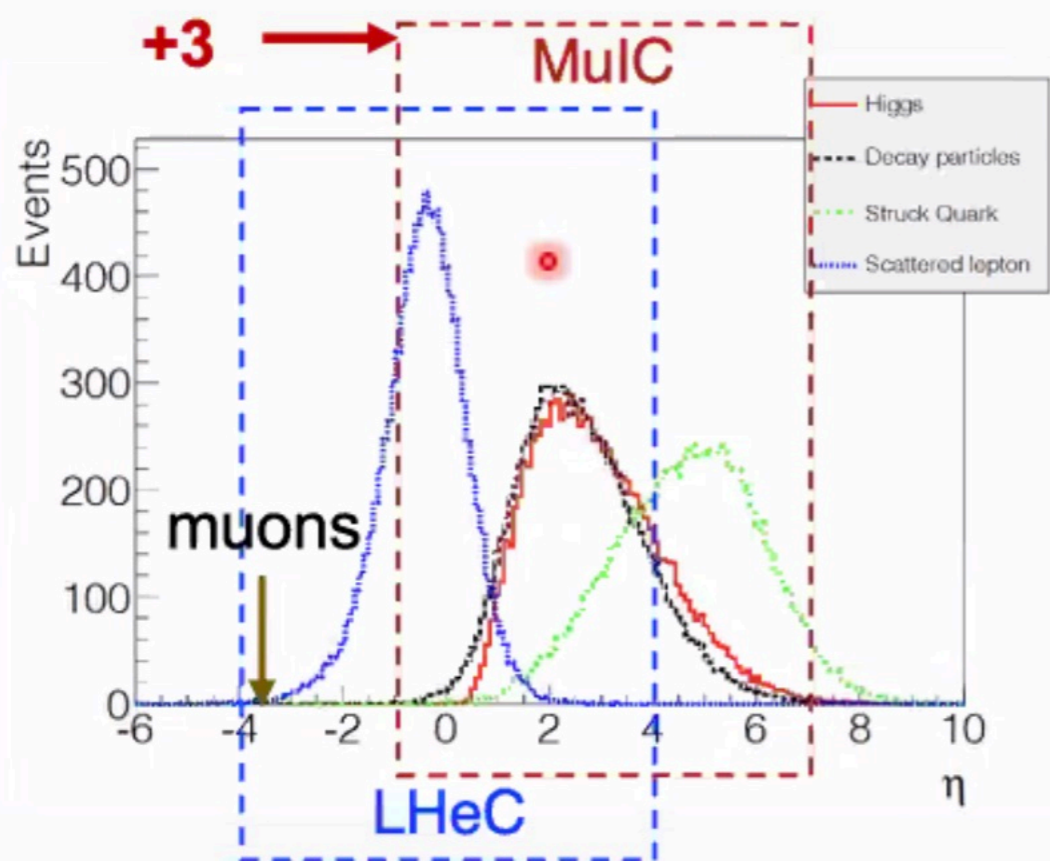
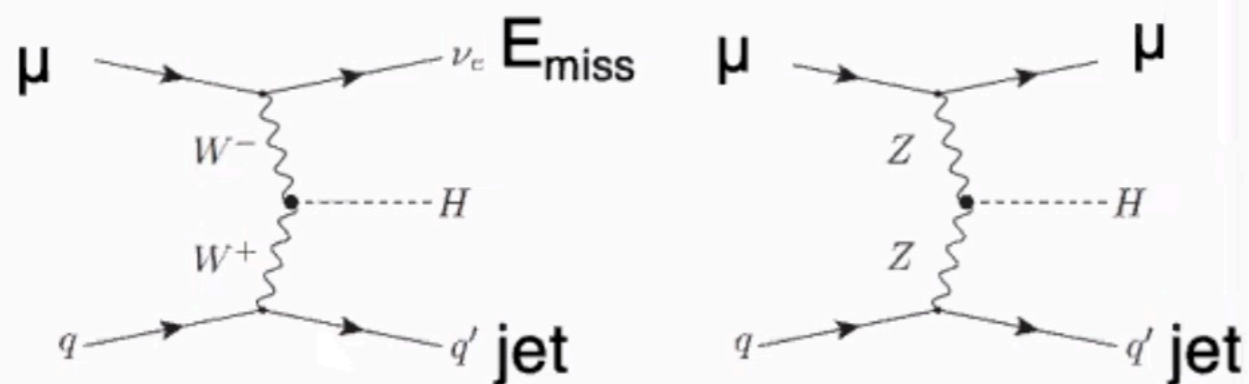


Uncertainties of Higgs couplings



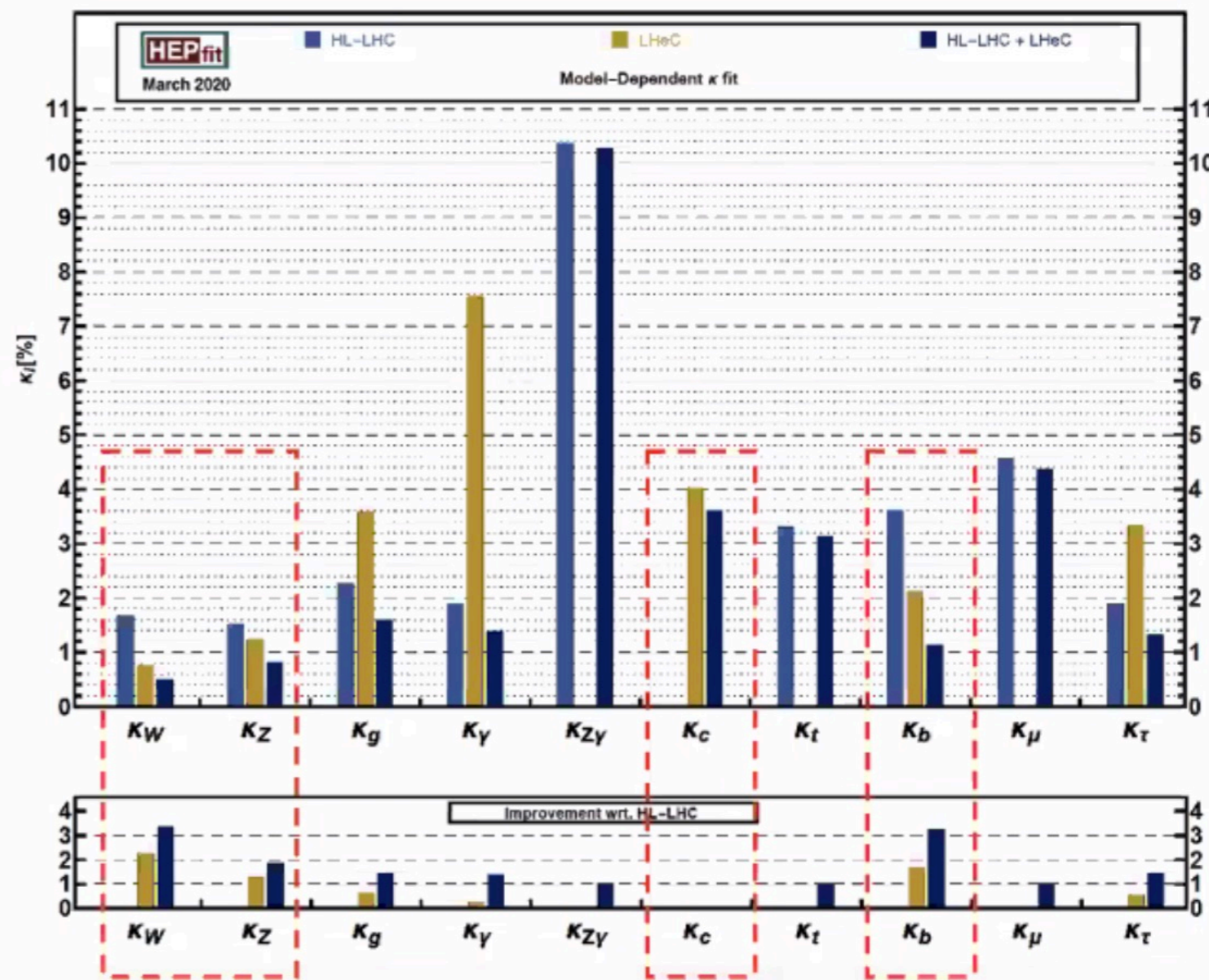
LHeC outperforms HL-LHC with $L_{\text{int}} = 1/\text{ab}$ in $\kappa_W, \kappa_Z, \kappa_b, \kappa_c$ Second generation

Higgs at the MuIC



At MuIC, kinematics for Higgs, jets more favorable but scattered muon is very forward.

Uncertainties of Higgs couplings

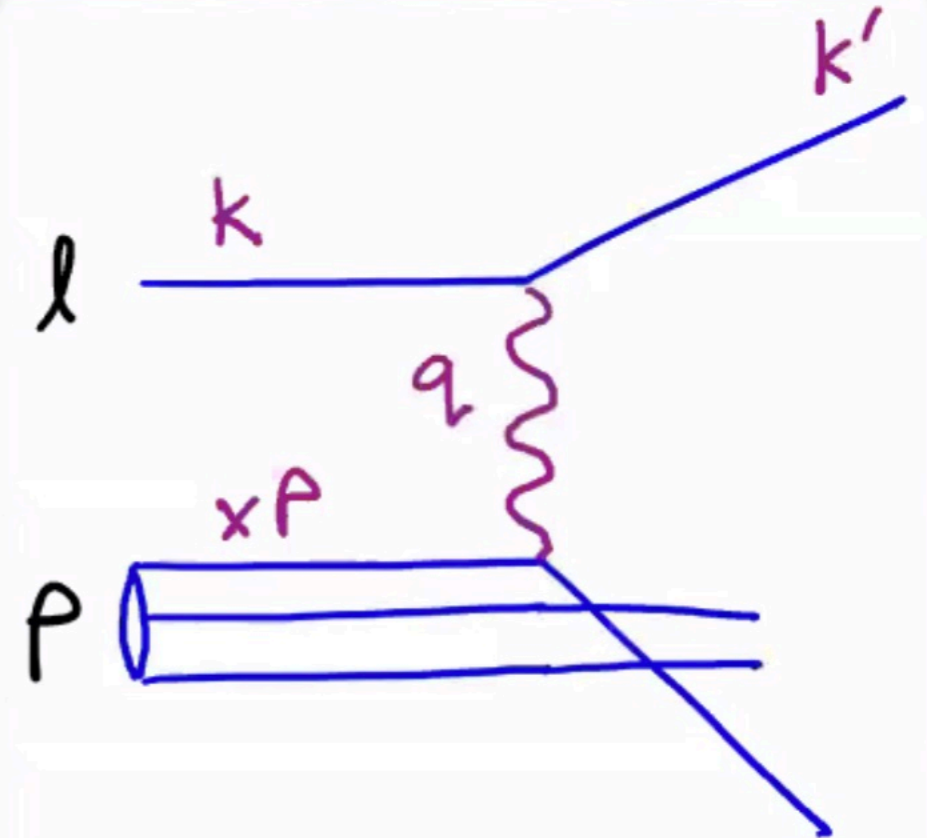


LHeC outperforms HL-LHC with $L_{\text{int}} = 1/\text{ab}$ in $\kappa_W, \kappa_Z, \kappa_b, \kappa_c$ **Second generation!**

DIS Variables and Kinematics



- $x = \frac{Q^2}{2P \cdot q}$ Bjorken x scaling variable
- $y = \frac{P \cdot q}{P \cdot k}$ Inelasticity
- $Q^2 \equiv -q^2 = -(k - k')^2 = sxy$ 4-mom transfer
- $s = (k + P)^2$ squared c.o.m. energy



From scattered lepton:

- $Q^2 = 2E_\ell E'_\ell (1 + \cos \theta)$

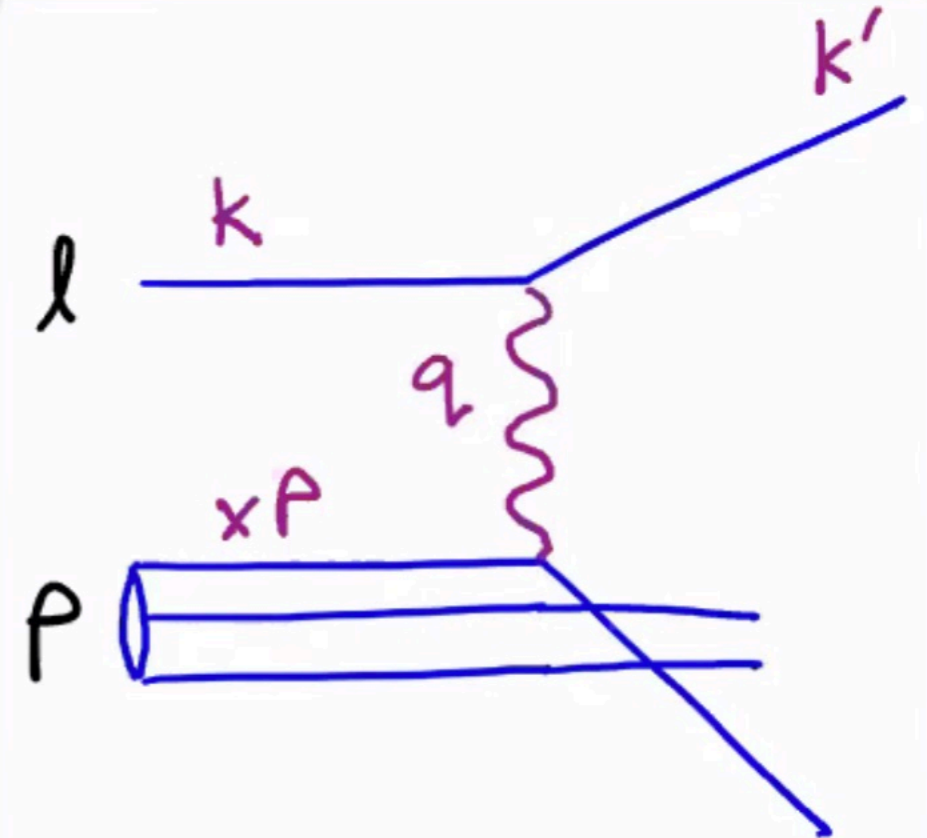
From scattered hadrons:

$$y = 1 - \frac{E'_\ell}{2E_\ell} (1 - \cos \theta)$$

DIS Variables and Kinematics



- $x = \frac{Q^2}{2P \cdot q}$ Bjorken x scaling variable
- $y = \frac{P \cdot q}{P \cdot k}$ Inelasticity
- $Q^2 \equiv -q^2 = -(k - k')^2 = sxy$ 4-mom transfer
- $s = (k + P)^2$ squared c.o.m. energy



θ is the polar angle w.r.t. the initial hadron direction

From scattered lepton:

- $Q^2 = 2E_\ell E'_\ell (1 + \cos \theta)$
- $y = 1 - \frac{E'_\ell}{2E_\ell} (1 - \cos \theta)$

From scattered hadrons:

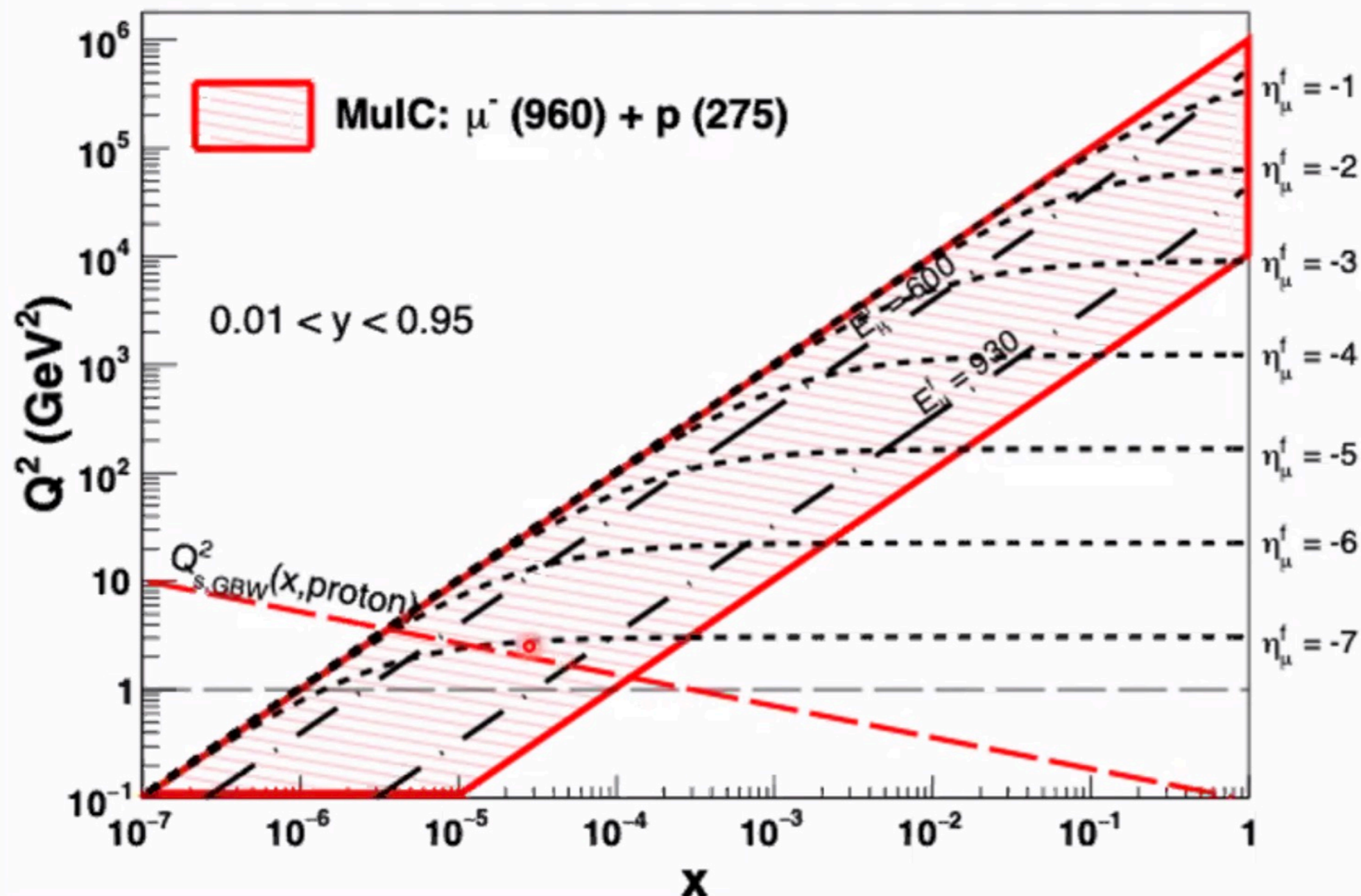
$$Q^2(P, \gamma) = \frac{P^2 \sin^2 \gamma}{1 - y(P, \gamma)}$$

$$y(P, \gamma) = \frac{P(1 - \cos \gamma)}{2E_\mu^i}$$

$$P^2 = (\sum_h P_h^x)^2 + (\sum_h P_h^y)^2 + (\sum_h P_h^z)^2,$$

$$\cos \gamma = \frac{(\sum_h P_h^x)^2 + (\sum_h P_h^y)^2 - (\sum_h (E_h - P_h^z))^2}{(\sum_h P_h^x)^2 + (\sum_h P_h^y)^2 + (\sum_h (E_h - P_h^z))^2}$$

Scattered Lepton Kinematics - MuIC



- Scattered muon momentum essentially defines y (decreases with y increasing)
 - **Typically > 500 GeV**
- Scattering angle is in very backward (lepton) direction
 - **$-7 < \eta < -5$ at low Q^2**

Distinct experimental challenges in tagging very forward muons to address.
(but hundreds of GeV muons will penetrate through anything, i.e. shielding)

Detector requirements and design



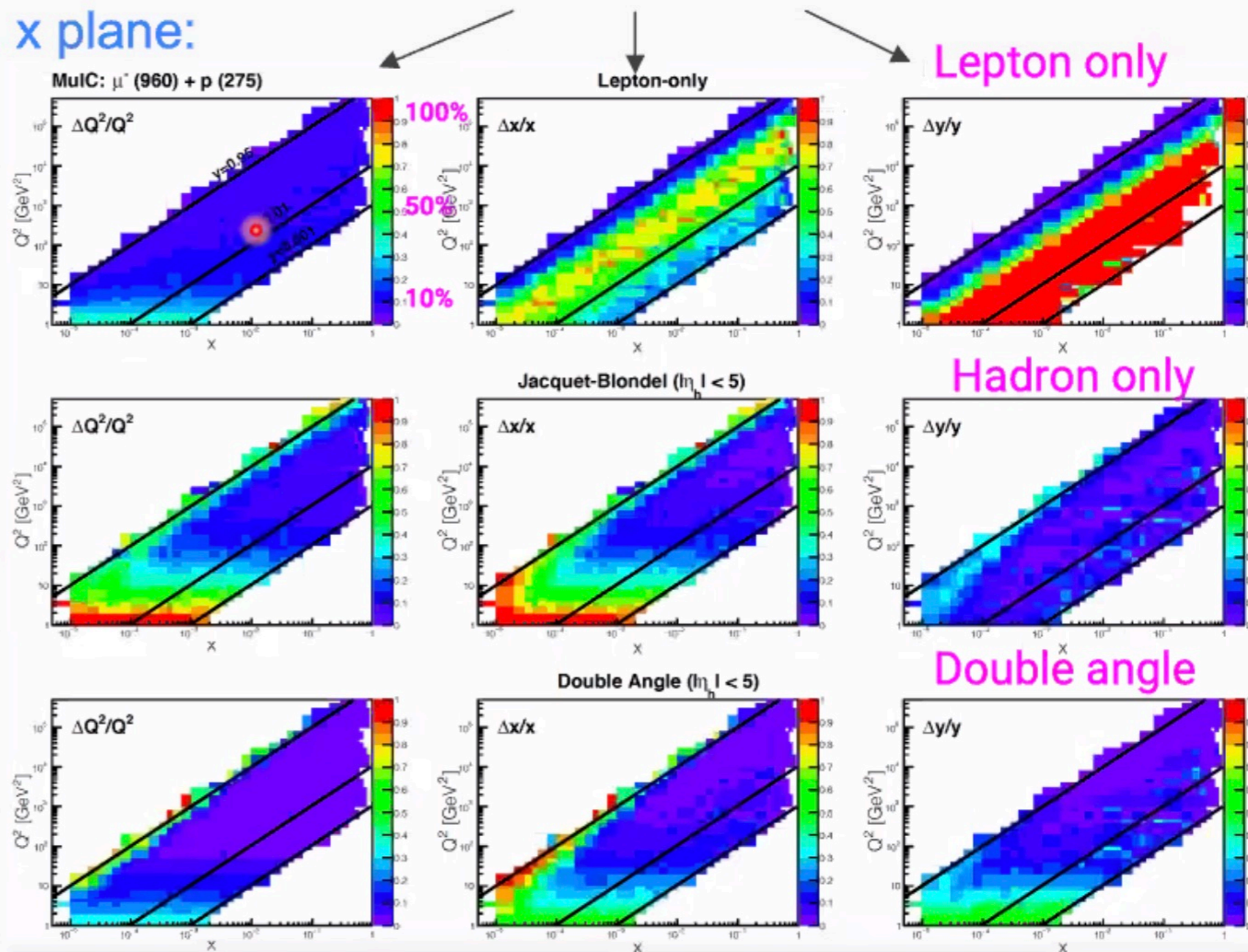
Resolutions of reconstructed Q^2 , x and y with 3 methods

Q^2 vs. x plane:

Simple assumptions of detector resolutions to smear particles from PYTHIA 8

Particle	Detector	Resolution	
		$\frac{\sigma(p)}{p}$ or $\frac{\sigma(E)}{E}$	$\sigma(\eta, \varphi)$
(Forward) Muons	e.g., MPGD	0.01% $p \oplus 1\%$	0.2×10^{-3}
Charged particles ($\pi^\pm, K^\pm, p/\bar{p}, e^\pm$)	Tracker + PID	0.1% $p \oplus 1\%$	$\left(\frac{2}{p} \oplus 0.2\right) \times 10^{-3}$
Photons	EM Calorimeter	$\frac{10\%}{\sqrt{E}} \oplus 2\%$	$\frac{0.087}{\sqrt{12}}$
Neutral hadrons (n, K_L^0)	Hadronic Calorimeter	$\frac{50\%}{\sqrt{E}} \oplus 10\%$	$\frac{0.087}{\sqrt{12}}$

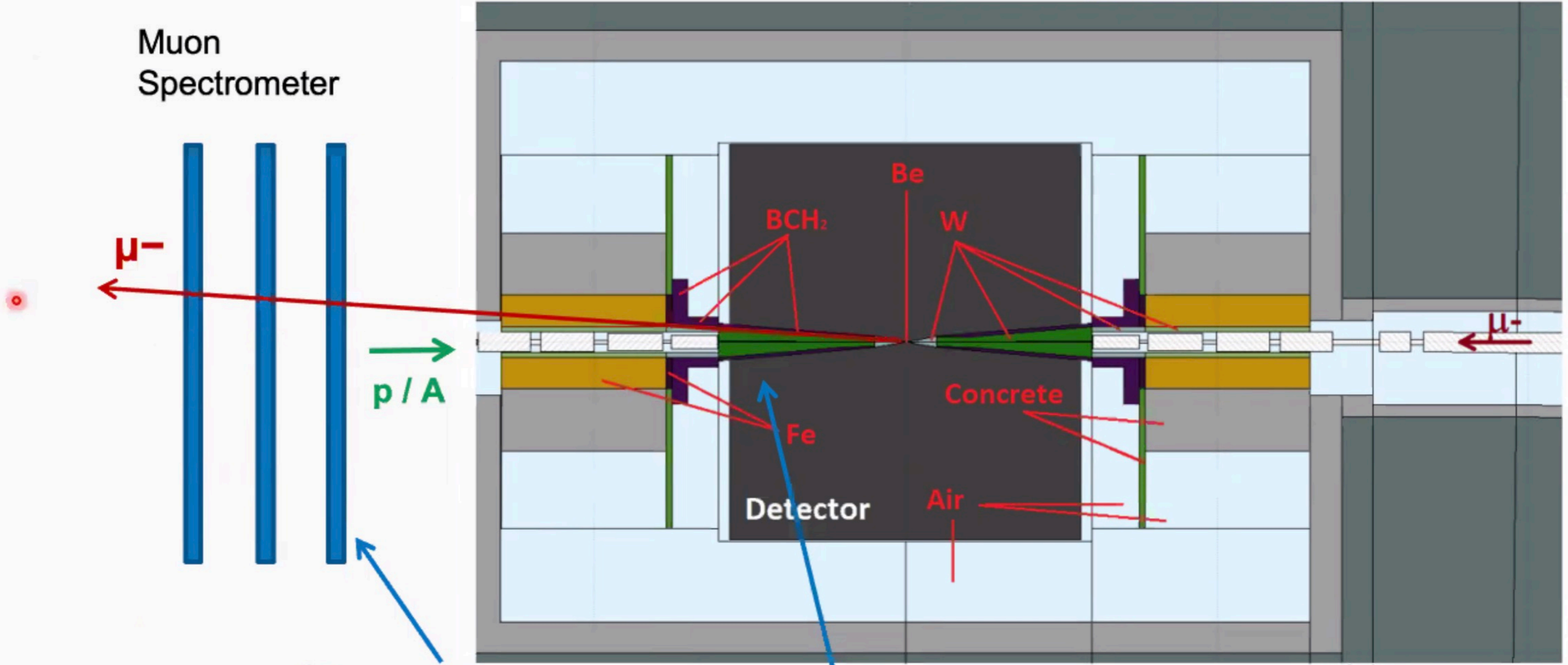
- Muons: 10% at 1 TeV, $\eta > -7$
- Hadrons: $|\eta| < 5$



Detector Design Considerations



From Collamati et al. on $\mu^+\mu^-$ collider: [arXiv:2105.09116](https://arxiv.org/abs/2105.09116)



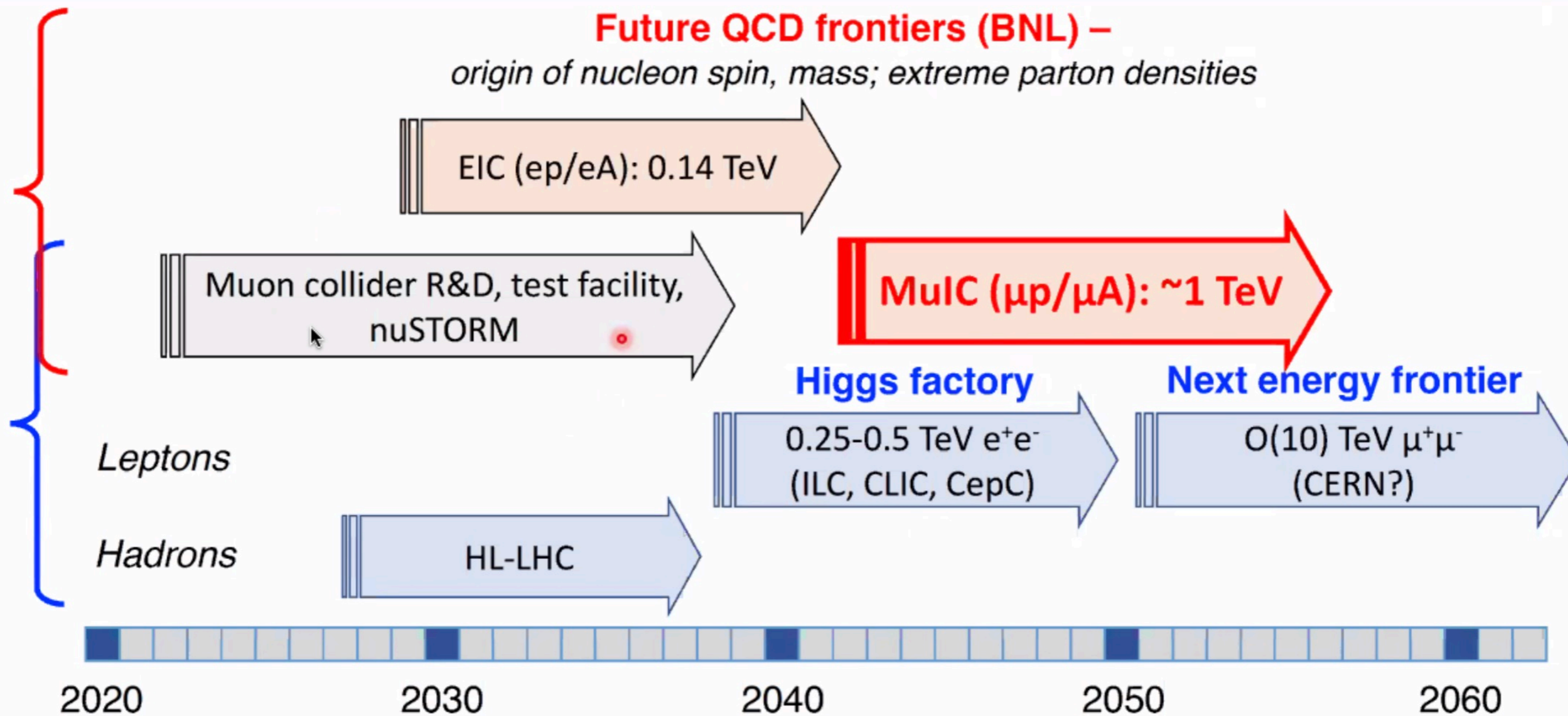
- Need a muon spectrometer
- Perhaps can reduce downstream shielding to improve hadron acceptance, as shielding nozzle may start at $|\eta| \sim 2.4$

Path forward (in our view)



NP

HEP

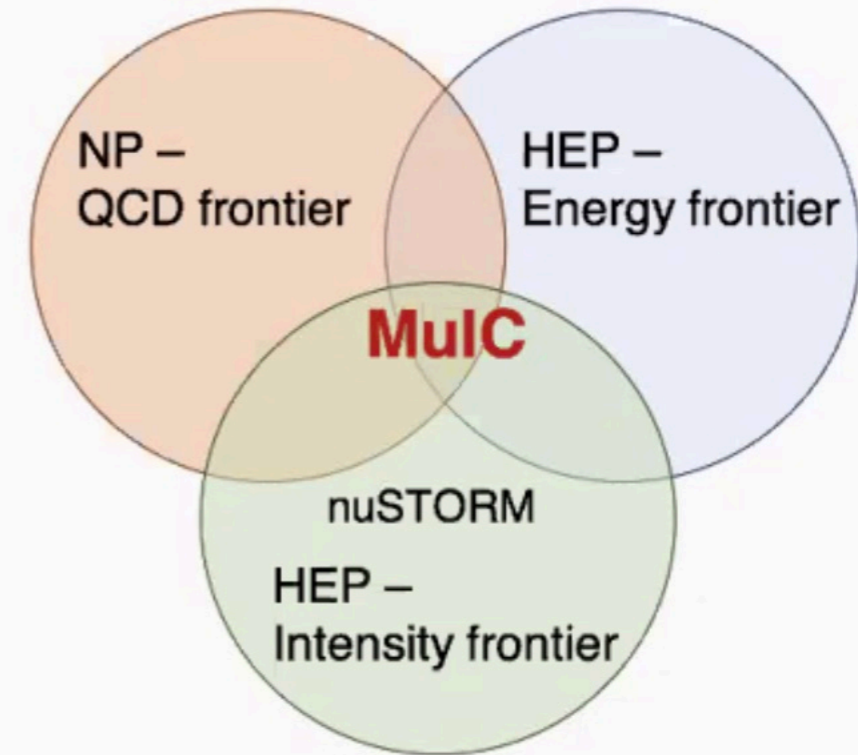


A possible roadmap to future muon colliders in NP and HEP



Key merits of MuIC concept:

- Compelling sciences with synergies across NP and HEP energy and intensity (e.g, [nuSTORM](#)) frontiers
- Serves as a demonstrator or staging option to establish the muon collider technology toward the ultimate $O(10+)$ TeV $\mu^+\mu^-$ (CERN?)
- Affordable as an “upgrade” to the EIC by re-using the existing facility, infrastructure, accelerator expertise
- A unique muon collider sited in US with a clear design goal by joint efforts of HEP and NP communities, and even attracting worldwide interests





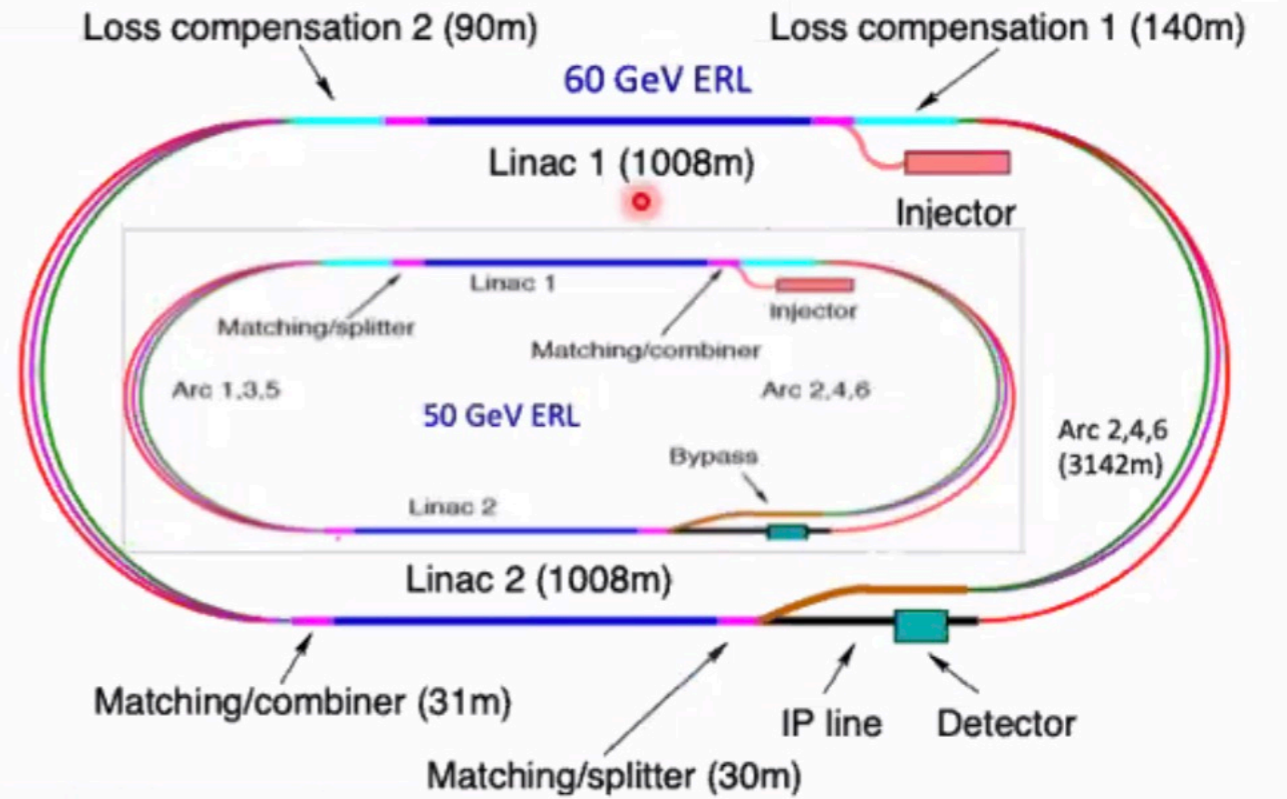
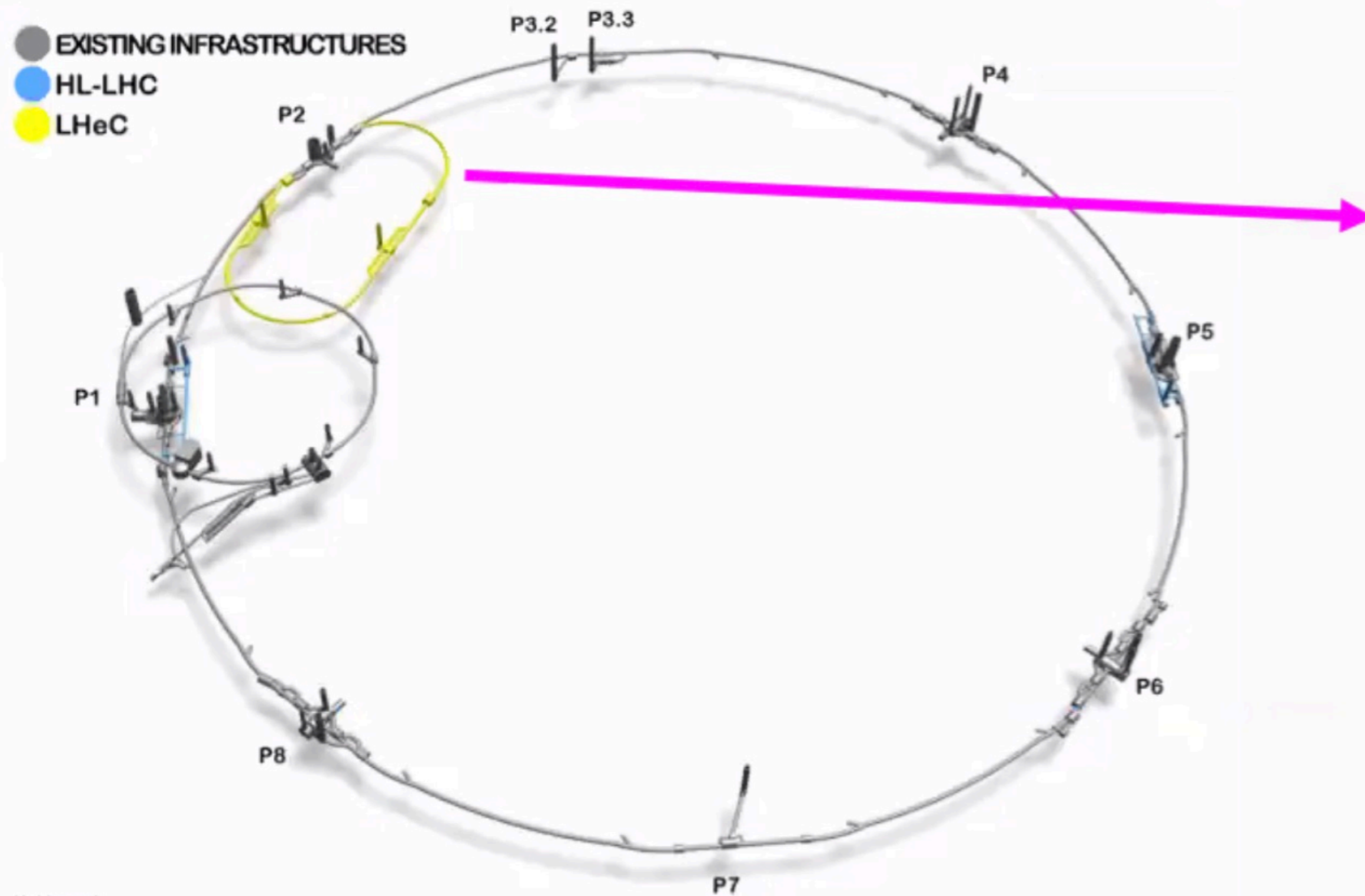
- Propose MuIC at BNL as one of future muon collider options in US to the Snowmass2021 planning exercise, and also propose the idea to the NP community in the upcoming long-range planning process in 2022
- Build on the MuIC concept, seek to establish dedicated R&D program on muon collider technology in US, involving HEP and NP in collaboration with the International Muon Collider Collaboration
- Engage BNL to consider MuIC as a future option of the lab, to start conceiving a possible design and potentially establish test facilities.
 - **Discuss with accelerator design experts on feasibility of muon acceleration at BNL facility**
- **Engage broader theoretical and experimental communities to explore the physics potential and to address detector design requirements/challenges (workshops, collaborations, and working groups)**

One Approach: Large Hadron Electron Collider



- **LHeC: 50 – 60 GeV e^- on 7 TeV p ($\sqrt{s} = 1.2-1.3$ TeV)**
 - Two oppositely directed linacs and 3 arcs
 - Two design options: 50 GeV (smaller) vs. 60 GeV (larger)

LHeC: [arXiv:2007.14491](https://arxiv.org/abs/2007.14491)



Not to scale

An Energy Frontier Muon Collider



A more compact and innovative facility to incorporate the advantages of a high precision lepton collider and an energy frontier machine

An $O(10)$ TeV muon collider has the equivalent mass reach to an $O(100)$ TeV proton collider

But much R&D still to do...

arXiv:1901.06150

